On the utility of pooling biological samples in microarray experiments

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Communicated by Grace Wahba, University of Wisconsin, Madison, WI, January 25, 2005 (received for review July 28, 2004)

Over 15% of the data sets catalogued in the Gene Expression Omnibus Database involve RNA samples that have been pooled before hybridization. Pooling affects data quality and inference, but the exact effects are not yet known because pooling has not been systematically studied in the context of microarray experiments. Here we report on the results of an experiment designed to evaluate the utility of pooling and the impact on identifying differentially expressed genes. We find that inference for most genes is not adversely affected by pooling, and we recommend that pooling be done when fewer than three arrays are used in each condition. For larger designs, pooling does not significantly improve inferences if few subjects are pooled. The realized benefits in this case do not outweigh the price paid for loss of individual specific information. Pooling is beneficial when many subjects are pooled, provided that independent samples contribute to multiple pools.

Messenger RNA samples are often pooled in a microarray experiment out of necessity (1, 2) or in an effort to reduce the effects of biological variation (3–6). The idea behind the latter motivation is that differences due to subject-to-subject variation will be minimized, making substantive features easier to find (7–13). This is often desirable when primary interest is not on the individual (e.g., making a prognosis or diagnosis), but rather on characteristics of the population from which certain individuals are obtained (e.g., identifying biomarkers or expression patterns common across individuals). Because pooled designs allow for measurement of groups of individuals using relatively few arrays, they have the potential to decrease costs when arrays are expensive relative to samples.

Despite the potential advantages, pooled designs are often discouraged because of concerns regarding the inability to identify and appropriately transform or remove aberrant subjects and the inability to estimate within population variation. These concerns are uncontroversial when all subjects in a study are pooled and only technical replicates are obtained. However, there are pooling strategies that compromise between pooling everything and only considering individual biological samples on individual arrays. Theoretical advantages of such designs have been established (10, 11, 14). A brief review is given here.

A microarray experiment to estimate gene expression levels consists of extraction and labeling of RNA from n subjects, hybridization to n arrays, followed by scanning and image processing. Assuming that sufficient data preprocessing has been done to remove artifacts within and across a set of arrays, the gene expression measurements for a gene denoted by x1, x2, ..., xn are considered independent and identically distributed samples from a distribution with mean θ, the quantity of interest. The average of the measurements is used to estimate θ. Because the processed measurements are affected primarily by biological and technical variation, denoted σ²b and σ²t, respectively, the xi are given by

\[ x_i = \theta + e_i + \xi_i \]
\[ = T_i + \xi_i \]

Assuming that RNAs average out when pooled (biological averaging), \( T_i = \frac{1}{r_s} \sum_{k=1}^{r_s} T_{ik} \) where rs denotes the number of subjects contributing RNA to a pool and T_{ik} is the kth subject’s contribution to the ith pool. Note that individual subjects contribute to one and only one pool, and in this way the pools contain biological replicates. Through biological averaging, the variability of \( e_i \) is reduced to \( \frac{\sigma^2_e}{r_s} \). The variance of the estimator for θ is then given by \( \frac{1}{n_p} (\sigma^2_e/r_s + \sigma^2_t/r_s) \), where np is the total number of pools and rs is the number of arrays probing each pool. The precision to estimate expression levels and the power to identify differentially expressed genes is inversely related to this variance, which is reduced by pooling because, for a pooled design, rs > 1. The larger biological variability is relative to technical variability, the larger the overall variance reduction and benefit of the pooled design.

The utility of pooling in practice depends on the extent to which the assumed conditions hold for microarray data. Previous studies provide limited support for biological averaging (6) and variance reduction in pools (13), whereas one study recommends not pooling at all (15). In the latter study, a design with 16 arrays (eight individuals in two conditions) is compared to one with 2 arrays (pool of eight in each condition). Clearly, because the number of arrays is decreased without increasing the number of subjects, the two designs are not comparable; and, furthermore, questions regarding gene identification cannot be answered without biological replicates of both individuals and pools.

In short, key questions regarding the pooling debate remain unresolved:

1. To what extent is variability reduced by pooling?
2. Is biological variability larger than technical variability for most genes?
3. To what extent does biological averaging hold?
4. Are inferences regarding differential expression comparable for pooled and nonpooled designs?

We report here on the results of a large Affymetrix experiment with individual and pools of varying sizes in two biological conditions designed to address these questions.

Methods

Supporting Information. For further details, see Supporting Text and Figs. 7–14, which are published as supporting information on the PNAS web site.

Data Collection. Thirty female inbred Wistar Furth rats were obtained from Harlan Sprague–Dawley at 5 weeks of age. The rats were group housed and provided Teklad diet (8604) and

Freely available online through the PNAS open access option.

Abbreviations: RMA, robust multarray analysis; DE, differentially expressed; FDR, false discovery rate.

Data Deposition: The microarray data reported in this paper have been deposited in the Gene Expression Omnibus database (accession no. GSE2331).
acidified water ad libitum. All rats were maintained with a light/dark cycle of 12 h. After a 2-week period of acclimation, rats were randomly assigned to a control or a retinoic X receptor treatment with an agonist LG100268, and were pair-fed every 24 h for 14 days. The experimental diets were prepared by adding LG100268, 100 mg per kg of diet meal (wt/wt), to the appropriate amount of ground rat meal diet and mixing for 15 min in an industrial size mixer in the chemical fume hood. All diets were double bagged and stored at −20°C for 1 week. Body weight was monitored by weighing at 2- or 3-day intervals. After consuming the diets for 14 days, rats were removed from the study for tissue collection.

RNA samples were obtained from 15 rats in each condition. The estrus stage of each rat is provided in the data supplement. Four RNA samples were not sufficient for hybridization (see Fig. 1). Affymetrix RAE230A chips were used to measure gene expression for 15,923 genes for the remaining 26 animals. A1 and B1 were removed after preliminary analysis because they were farthest from other arrays in dendrograms similar to those shown in Figs. 8–10. The remaining 12 from each condition were chosen to construct 12 pools of pairs, 8 pools of triples, and 2 pools of 12 subjects. To obtain cRNA samples, total RNA was extracted from individual mammary glands; 5 μg of each RNA sample was reverse transcribed, synthesized to double-stranded cDNA, and then transcribed to biotin-labeled cRNA targets which were then fragmented. For the individuals, each chip was hybridized by using 10 μg of the fragmented cRNA targets; for the pools, equal amounts of fragmented targets were combined from the individuals to give a total of 10 μg. We note that the pooling was done after the labeling reactions, primarily to ensure enough starting material for individuals and multiple pools. When lack of sufficient tissue motivates pooling, samples would be combined before labeling and results could differ from those presented here. Within pool group, the processing of samples was randomized across treatments and Affymetrix scanners. To estimate technical variability, A3, B3, AQ, and BQ were analyzed using additional microarrays. Fig. 1 gives a schematic of the experiment. A single individual sample hybridized onto a single array is referred to as “1 on 1”; a pool of n subjects hybridized onto a single array is “n on 1”; M = np × n unique subjects hybridized onto np arrays (a pool of n onto each array) will be referred to as “M on np.” N technical replicates of a single array containing n subjects are denoted by “n on 1×N.”

Preprocessing and Normalization. Robust multiarray analysis (RMA) was used to preprocess and normalize the raw Affymetrix GeneChip data (16). Individuals, pools, and technical replicates were processed together. RMA fits a linear model to the log probe intensities for each probe set. The linear model includes a sample effect, a probe effect, and an error term. Fig. 7 shows standard error estimates of the sample effects for each array. Because RMA has been shown to give very low false-positive rates without filtering, and potentially inflated false-negative rates after filtering, all 15,923 genes were used in the analysis. RMA has been demonstrated to provide improved precision over the default algorithms provided by Affymetrix, which generates MAS5.0 signals (17). We observe similar findings for this data set (Figs. 8–10).

Comparison of Designs. For each design, moderated t statistics (18) between control and treatment samples were obtained for every gene if more than three arrays were available (see Supporting Text). With fewer than three arrays, a fold change was calculated. For the rank plot (see Fig. 6A), the statistics were ranked from largest to smallest. The top N genes made up a list of size N. For the false discovery rate (FDR) plot (see Fig. 6B), the FDR of a
Results

Fig. 2. Gene-specific sample variances: cumulative distribution functions of gene specific sample variances are calculated by combining estimates across biological conditions. Density estimates are shown in Fig. 11.

Pooling Reduces Overall Variability. Gene-specific sample variances were calculated across conditions for individual samples, pools of 2 and 3, and technical replicates. Fig. 2 shows nearly perfect stochastic ordering with decreasing variability from individuals to technical replicates. However, this trend does not hold for each gene. Variability across technical replicates was larger than variability across individuals for 31% of the genes. The negligible biological variability estimated here may be due to truly small biological variability or to poorly designed probe sets that allow for little hybridization or sufficient cross-hybridization. Whatever the reason, for genes with relatively small biological variability, there are negligible gains by pooling.

Pooling Results in Biological Averaging for Most Genes. To investigate whether RNA samples average out when pooled (biological averaging), mathematical averages (referred to here as averages) across individuals were compared to the corresponding pools. Some distortion is expected as the original RNA abundance undergoes a series of possibly nonlinear transformations during the measurement process. In the absence of pooling, individual samples are transformed separately, whereas when pooling is done, the transformation applies to the pool rather than to each individual sample. Any averaging that takes place on the scale of raw RNA abundance is transformed during data generation and processing, and as a result measurements from a pool may not correspond to an average of individual samples that comprise the pool.

Fig. 3 gives an example. Shown is one gene where the averages on the raw intensity scale are quite similar across the individuals and pools. After a log transformation, as often recommended for microarray data (20–25), the averages in the individuals are smaller than those in the pools. This is a biological realization of the well known Jensen’s inequality (26), which states that the average of log transformed values will always be less than or equal to the log of the average of the untransformed values. The fact that we observe this difference here is evidence of biological averaging (pools look like an average of untransformed individual values). The difference between the average of the log individuals and the log of the pools is exacerbated by outliers (e.g., arrays 3 and 10 in Fig. 3). Part of the reason for this is that for the case of individuals, outliers are first attenuated by a log transform and then averaged. For the pools, the attenuation has less of an effect because the outlier has already been averaged with other samples. Fig. 4A shows that this artifact affects ~25% of the genes.

Another factor potentially affecting agreement between pools and their averages is that the actual amount of individual RNA contributing to each pool may vary across individuals, despite careful quality control measures. The effects of this on pooling have been considered (27). Despite distortions, we find that pools are more similar to averages of the contributing samples than they are to other pools (Fig. 13). Furthermore, the dendrogram in Fig. 9 shows that pools of two cluster closely with their averages. The same holds for pools of three. These plots suggest that biological averaging occurs for most, but not all genes. Furthermore, for the genes where biological averaging does not occur, similar amounts of distortion are often observed.
in both control and treatment conditions and, as a result, the identification of DE genes is not grossly affected (Fig. 4).

Identifying Differentially Expressed Genes. Designs without biological replicates. Without biological replication, outliers cannot be found and appropriate variance components cannot be estimated. Fig. 5 gives an example of how this can adversely affect DE inferences. Each affected gene appears to be DE when only technical replicates are considered. It is clear when biological replicates are available that the first DE call is caused by outliers and the second DE call is caused by an underestimation of the gene-specific variance. The last gene shown is not affected by an outlier. Correct inferences regarding DE would be made in this case using only technical replicates. Fig. 6 shows that this latter case is most representative of the full data set as similar lists of DE genes are identified when using true biological replicates (e.g., 12 on 4/11015 12 on 1/11003 4; see Methods for terminology). In fact, the same level of accuracy is only slightly reduced when single arrays with pools of 12 (12 on 1) are considered. This is not the case when pooling is not done. An analysis using individuals on single arrays (1 on 1) reduces accuracy by 50%.

Pooled designs with biological replication. When the RNA from an individual contributes to one and only one pool, and many pools are constructed, the pools can be used to properly assess biological variation. Pooling extra subjects onto a fixed number of arrays decreases variability across experiments and provides a representative list of genes with accuracy similar to the representative lists obtained without pooling (Fig. 6A). For example, the representative lists from an analysis of 3 on 3, 6 on 3, or 9 on 3 have similar accuracy. However, the variability across the 9 on 3 experiments is reduced, resulting in a list for a particular experiment that has properties near those of the representative list. Similar results are found for other comparisons. Reducing the number of arrays in an experiment without increasing the number of subjects decreases accuracy (Fig. 6A).

False discovery rate (FDR) control. Designs in Fig. 6A are compared based on agreement among the top ranking genes for lists with fixed size. For these comparisons, no consideration of the FDR associated with each list is made. Results regarding accuracy are very similar when comparisons are instead made among
lists with fixed FDR. There is one major difference: when biological replicates are not available and technical replicates are used, estimates of the variance required for FDR specification are incorrect, resulting in many DE calls with very low accuracy (Fig. 6B). Fig. 6B also provides insight into how the number of genes identified as DE by an FDR-based criterion varies among the designs. As the number of arrays decreases for a fixed number of subjects, fewer genes are identified as DE. This reduction is expected, because to have comparable results while decreasing the number of arrays, one must increase the number of subjects appropriately to maintain a so-called “equivalent” design.

Equivalent designs. Formulas exist specifying the number of subjects and arrays required in a pooled design so that gene specific (10) or average (11) estimation efficiency is maintained comparable to a design where pooling is not done and additional arrays are used (see Supporting Text). Similar formulas hold when equivalent power is considered. Given the biological and technical variability in this study, the following designs are equivalent: 100 on 100 vs. 160 on 80; 25 on 25 vs. 42 on 21; 7 on 7 vs. 12 on 6. Fig. 14 shows that there is little difference between the genes identified from the last designs. However, although the designs are equivalent on average, gene-specific DE calls are affected by varying biological and technical variability; and, as a result, pooling while reducing the number of arrays will be useful for identifying some genes, at the expense of not identifying others.

Discussion

Experimental designs using pooled RNA samples are often done out of necessity or in an effort to reduce the effects of biological variation, making substantive differences easier to find. Pooled designs are attractive because they have the potential to decrease cost due to the fact that a large number of individual samples can be evaluated using relatively few arrays. Here, we have considered fundamental properties of various pooling designs to evaluate their performance and to determine whether the basic conditions required for pooling to be useful hold.

The most basic condition is the assumption of biological averaging. Many investigators conjecture that RNA abundance levels average out when pooled. This may be true; however, because of nonlinearities introduced in the generation and processing of microarray data, an average on the scale of raw RNA abundance will not necessarily correspond to the average of the same highly processed RNA measurements. The log transformation was found to affect ≈25% of the genes (some distortion also appears on the raw intensity scale; this is not considered here because data are almost always transformed before analysis; refs. 20–25). There may also be implicit transformations that could affect the measurements; despite these, we found that most expression measurements from RNA pools are similar to averages of individuals that comprise the pool. For the majority of genes where there was a large difference, the difference was similar across biological conditions, resulting in comparable DE inferences from individuals and pools. Because of this, pooled designs were never found to perform significantly worse than nonpooled designs.

For very small designs in which only one or two arrays are available in each biological condition, pooling dramatically improves accuracy. Although valid, the results in such small designs are limited as gene specific variance components cannot be well estimated and outliers cannot be identified. Designs involving technical replicates only are similarly limited; and when used with statistical methods that require estimates of both biological and technical variability (e.g., FDR-based methods), they can be very misleading. When the goal of the experiment is to identify DE genes, investigators should favor biological, not technical, replicates.

For larger designs where biological replicates are used, pooling is not always advantageous. Accuracy was similar across designs in both the rank and FDR based analyses when the number of arrays was fixed and the number of subjects varied. There is a slight decrease in the variability among the lists of DE genes identified as the number of subjects pooled increased; but the modest reduction resulting from pooling two to three subjects per array is generally not worth the price paid for loss of individual specific information. A greater advantage can be gained by pooling a larger number of subjects. For a fixed number of subjects, reducing the number of arrays results in decreasing accuracy and fewer genes with small FDR. This result is expected, because to maintain equivalent properties, the number of subjects pooled must be increased appropriately.

An optimal method for specifying equivalent designs will depend on a number of factors (see Supporting Text). To the
extent that simplified models of equivalence hold (10, 11), we
found the following designs to be equivalent for this data set: 100 on 100 vs. 160 on 80; 25 on 25 vs. 42 on 21; 7 on 7 vs. 12 on 6; evidence for equivalence was given in the last case. The
financial benefit of pooling for this particular case is minimal
at best. However, the results demonstrate the potential of
equivalent design specification. For larger designs, the realized
benefit of decreasing the number of arrays can be substantial.
Furthermore, in studies of humans, biological variability is
generally larger than technical variability (28), the condition
that yields a greater reduction in the number of arrays
required. Experiments to estimate gene-specific variance com-
ponents and validate the conditions considered here should
prove quite useful for extrapolating these results to other
systems and addressing other questions of microarray exper-
imental design.

We thank Eric Blalock, Gary Churchill, and Michael Newton for useful
discussions and two anonymous referees for comments that greatly
improved the manuscript. Our special thanks go to Ray Carroll, who
couraged C.K. to apply for National Institutes of Health Grant
R03-CA103522, which funded this experiment. M.N.G. was supported in
part by National Institutes of Health Grant R01-CA101201.

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