Estimating enhanced prevaccination measles transmission hotspots in the context of cross-scale dynamics

Alexander D. Becker<sup>a,1</sup>, Ruthie B. Birger<sup>a</sup>, Aude Teillant<sup>b</sup>, Paul A. Gastanaduy<sup>b</sup>, Gregory S. Wallace<sup>b</sup>, and Bryan T. Grenfell<sup>a,c,d</sup>

<sup>a</sup>Department of Ecology and Evolutionary Biology, Princeton University, Princeton, NJ 08544; <sup>b</sup>Division of Viral Disease, National Center for Immunization and Respiratory Diseases, Centers for Disease Control, Atlanta, GA 30329; <sup>c</sup>Woodrow Wilson School of Public and International Affairs, Princeton University, Princeton, NJ 08544; and <sup>d</sup>Fogarty International Center, National Institutes of Health, Bethesda, MD 20892

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A key question in clarifying human–environment interactions is how dynamic complexity develops across integrative scales from molecular to population and global levels. Apart from its public health importance, measles is an excellent test bed for such an analysis. Simple mechanistic models have successfully illuminated measles dynamics at the city and country levels, revealing seasonal forcing of transmission as a major driver of long-term epidemic behavior. Seasonal forcing ties closely to patterns of school aggregation at the individual and community levels, but there are few explicit estimates of school transmission due to the relative lack of epidemic data at this scale. Here, we use data from a 1904 measles outbreak in schools in Woolwich, London, coupled with a stochastic Susceptible-Infected-Recovered model to analyze measles incidence data. Our results indicate that transmission within schools and age classes is higher than previous population-level serological data would suggest. This analysis sheds quantitative light on the role of school-aged children in measles cross-scale dynamics, as we illustrate with references to the contemporary vaccination landscape.

The dynamics of measles are a paradigm for the emergence of algorithmically simple (albeit often dynamically complex) host–natural enemy cycles (1). At the most predictable scales, the Susceptible-Infected-Recovered (SIR) family of models has been used to analyze measles dynamics in city and country metapopulations (1–4), as well as in allowing for heterogeneities in space (5, 6), age (7, 8), and population sizes (9, 10). As a badge of simplicity, SIR models successfully assume well-mixed mass action in city populations (i.e., that the number of individuals who will become infected is proportional to the total number currently infected as well as those currently susceptible). Mass-action assumptions can use a simple constant contact rate or use a complex time-varying contact function to capture seasonality.

The time dependency (or lack thereof) of the contact rate is determined by the temporal scale of the data. For example, prevaccination measles is characterized by strong multiennial (1) epidemics (Fig. L4; reported case counts from London) that were driven by the increased seasonal contact rate between children during the school term (7, 11, 12). The contact rate is in the numerator of expressions for the basic reproductive ratio 

$$R_0,$$

which measures the number of secondary cases per infected individual in a fully susceptible population. This measure informs various quantities important for public health such as timing of epidemic peaks and what proportion of the population must be vaccinated to prevent an outbreak (13). 

$$R_0$$ estimates for measles are frequently reported as being between 7 and 18 (13, 14), consistent with an average age at first infection of 4 to 10 y. However, because serology is generally reported in broad age bands, it may smooth out the sharpness of school epidemics, as reflected in recent studies that argue that higher 

$$R_0$$ values (15) inferred from time-series data reflect transmission within schools rather than the actual population-level average (4, 14, 16), underscoring the importance of school-age children in a population-level outbreak.

The cross-scale dynamics of measles are summarized schematically in Fig. 1. We see more complexities, and often violent “superspreader” dynamics, emerge at the underlying micro scales of schools and families (e.g., Fig. 1 C and D). Fig. 1C (data from Woolwich, London analyzed in this paper) shows outbreaks from three schools (colored lines), which combine into a highly stochastic school-level time series (dashed black). Fig. 1D schematically illustrates family-to-family transmission, which can connect school epidemics. These micro outbreaks can be explored using both mass-action and network models (17). The school and family outbreaks scale up to local community level (Fig. 1B); these outbreaks have traditionally been studied with network models (17). However, few studies have examined the transmission hotspots that add up to the “emergent simplicity” of the population-level dynamics.

One notable exception is the exquisitely detailed dataset from an 1861 measles outbreak in Hagelloch, Germany, during which all 188 susceptible children in the village became infected. With fine-grain information such as family units, house location, and which classroom each child was in recorded, the Hagelloch outbreak has been extensively studied using network models, and 

$$R_0$$ has been estimated to be in the range of 6 to 19 (17–19). However, 1861 Hagelloch was a small population, bearing little resemblance to a city such as London. It is therefore difficult to extrapolate the Hagelloch transmission in the context of school outbreaks in a large city. Additionally, there were only two school epidemics in Hagelloch, so there are no estimates of 

$$R_0$$ variability (20).

Schools act as measles transmission hotspots, and such deviations from the average are especially important, as noted in the work of Lloyd-Smith et al. (20) on superspreading. Unfortunately, measles outbreaks in schools are not a relic of...
the prevaccination era (21). Although vaccine coverage in most US schools is high, vaccine refusal and personal belief exemptions trends are increasing (22, 23), leading to considerable variability in vaccination rates (21, 24), and measles susceptibility rates in some US kindergartens are below the critical coverage (25). In this paper, we aim to illuminate the dynamics of school-based measles transmission by analyzing detailed data from a 1904 measles outbreak across several schools in Woolwich, London. First, we present the data and difficulties associated with fitting school-level incidence data for measles. We then fit a stochastic SIR model to the data to estimate transmission in schools and age classes. We then discuss the role of school children in city-level results. Finally, we investigate the implications of our findings for recently reported heterogeneities in California school vaccination rates as an example of the transmissibility that could be observed in schools in other states with variable vaccination coverage. We conclude by discussing the general implication of these results for cross-scale dynamics in epidemiology and ecology.

Results

Measles in 1904. For the school-level data we estimate an average \( R_0 = 27 \) with range (12, 42), an average reporting ratio \( \rho = 70\% \) with range (17%, 95%), and an average dispersion of the negative binomial \( \psi = 0.92 \) with range (0.83, 0.99). The age-class data show similar, although reduced, transmission variability, with an average \( R_0 = 40 \) and a range of (8, 93). The average estimated reporting rate is \( \rho = 72\% \) with a range of (37%, 91%) and the average dispersion of the negative binomial \( \psi \) was estimated to be 0.83 with range (0.70, 0.94). These results are shown in Fig. 2 B–D. The number of time series used for the school level was \( n = 6 \), and \( n = 12 \) for the age level. For both datasets the high dispersion estimates indicate a high degree of variability in the reporting rates.

For \( R_0 \), \( \rho \), and \( \psi \) we run \( t \) tests to determine how different the estimates for the school versus the age groups are based on the means. No \( t \) test results came out statistically significant except for the \( \psi \) estimates (\( P = 0.02581 \)). We did not detect a significant difference in the means of the \( R_0 \) and \( \rho \) estimates for schools versus age classes. However, differences in the dispersion parameter \( \psi \) indicate there may be variability in underreporting in schools and age classes.

Resimulating the model using the estimated parameters yields generally close fits (using \( R^2 \) as a simple estimate) to the data, as seen in Figs. 3 and 4. For the school data, the adjusted \( R^2 \) range is 0.3 to 0.87, with all \( P \) values statistically significant with the exception of Vicarage Road. For the age data, the adjusted \( R^2 \) range is 0.076 to 0.94, with all \( P \) values statistically significant with the exception of Maryon Park, age 3. If that exception is removed, the adjusted \( R^2 \) range increases to 0.37 to 0.94. There was no clear trend between \( R_0 \) estimates and school size or age class. These results can be seen in Supporting Information.

Measles in 2016. Our results and \( R_0 \) estimates showcase the potential effects of a lowered vaccine coverage. Fig. 5 shows the range of potential outbreak final sizes for varying vaccination coverage levels using \( R_0 \) values consistent with those found in this study. The lowest \( R_0 \) value, 5, is used to take into account potential control measures. Predicted outbreak sizes are in the range of 10 to over 50 cases for a school size of 77, reflecting an average across over 7,000 kindergartens in California (25). Many individual schools in California have been below the critical vaccination threshold for measles, indicating a large risk (21, 24, 25). Mean up-to-date coverage in 2015–2016 in California kindergartens was 93% with a 5 to 95 percentile range of 73 to 100% and minimum and maximum coverage levels of 5 to 100% (25). The shaded region in Fig. 5 indicates this 5 to 95 percentile range, although it does not include the over 300 schools whose coverage is below the fifth percentile, and whose average coverage level is just over 55% (25). Here we assume 100% vaccine efficacy. These results indicate the possibility of very large outbreaks building in the postvaccine era.
Discussion
Understanding the processes that underlie large-scale dynamics of a complex, multilevel system can lend valuable insight into the transition of complexity across scales (27). Here, this transition refers to how large-scale aggregation of incidence data can produce relatively predictable patterns. Seasonal forcing determined by the school calendar is known to be an important driver of measles dynamics. Here, we underpin this phenomenon with direct analysis of school-level data, demonstrating very high pre-vaccination transmission within schools and age classes. Our results highlight differences in age-specific transmission, thus demonstrating the importance of school transmission hotspots (15). Recalling that traditional population-level estimates of $R_0$ values are between 7 and 18 (13, 14), we confirm hypotheses that higher estimates based on time-series data are effectively picking up transmission within the schools. On the low end of the school and age estimates, our $R_0$ values are similar to those from the Hagelloch dataset. However, the Hagelloch $R_0$ was derived from the community-level data, whereas the Hagelloch classroom data show a much faster spread of infection, which would support a higher $R_0$, in line with the results presented in this paper.

Although an $R_0$ of 93 is extremely high, written accounts of these outbreaks may support even higher values. In a 1905 measles report on the Education Committee of the London County Council, Dr. Kerr reports an incident in which a Woolwich child of 5 y “in spite of prompt and energetic measures, may be said to have caused at least 207 known cases in four schools” (28). However, it is not completely clear whether...
Fig. 5. A simulation showing the variation in outbreak final size for a range of $R_0$ values over increasing proportion susceptible/decreasing proportion vaccinated. The shaded region indicates a 95% range of MMR (measles, mumps, and rubella) vaccination coverage in schools in California, demonstrating that the risk of outbreaks is still present in the postvaccination era (26).

this account refers to direct transmission or the child’s transmission tree (28). Furthermore, this is in line with the famous 1951 Greenland epidemic in which one person infected over 200 others (29). The Greenland epidemic was used in Lloyd-Smith et al.’s (20) important study of epidemic superspreaders. Looking at transmission variability, Lloyd-Smith et al. (20) estimated the negative binomial dispersion for $R_0$ variability parameter, $k$, as $<0.1$ for measles. In this context, a small $k$ indicates a high degree of transmission variability where superspreaders drive the majority of the outbreak. Using the distribution of the 18 inferred $R_0$, we calculate $k = 1.3$ via a moment estimate, indicating less transmission variability than the Lloyd-Smith et al. (20) estimate. However, here we are fitting the upper tail of transmission of the epidemic size range, so our results are likely to underestimate overdispersion. Our estimated reporting rates are slightly higher than previous estimates such as 51% in ref. 1 and 13–78% in ref. 4, which may be due to the attention given to documenting the 1904 outbreaks.

Applying the low end of the school transmission to the current vaccine landscape in California schools yields an unsettling implication for outbreaks (Fig. 5). In some cases, vaccination coverage may be underestimated, because children with nonmedical vaccine exemptions often do not have their true vaccination status assessed (30). Individual school vaccination coverage levels may be slightly higher than reports indicate; ref. 30 estimates that 10–50% of children with personal belief exemptions (PBEs) may actually have received a full MMR vaccination course, so Fig. 5 may be conservatively pessimistic. Nonetheless, even if 50% of children with PBEs are covered, coverage in many schools would still be well below the herd immunity threshold for measles. If a measles outbreak were to occur in just one or a few of the low-coverage schools, the resulting epidemic final sizes could approach annual numbers of measles cases reported in the United States (ranging from $\sim50$ to $\sim700$ between 2010 and 2015) (31). Effectively, herd immunity for measles really is a measure of whether measles can be kept out of the school, and limitation of establishment of endemicity. Once measles is in a school, it will find and infect susceptible individuals with great efficiency.

Our study, and the data themselves, have a number of limitations. First, within our school population we assume homogeneous mixing, although some studies have suggested that even within school-age children contact is not constant (32). Second, in our model we do not account for time-dependent imported infections, which may account for a number of school-level outbreaks. In a similar vein, we do not consider the role of family and siblings in our study. In the same Education Committee of the London County Council report, Dr. Kerr states that infection may have been spread between age classes because older children often walked younger students home (28). Additionally, these import infections may help to explain the appearance of noise in our datasets that rendered a significant number of the time series unusable under our well-mixed assumption—indicating that perhaps a network or spatial compartmental model could be of use in future analysis of this dataset. We also assume that contemporary California schools resemble early 20th-century London schools in ways that are important for measles transmission (i.e., class sizes and homogeneous transmission within the age classes and schools). Additionally, we only applied the low end of the London $R_0$ esti-
mates to modern California, even using $R_0 = 5$ to account for control measures. However, even with these limitations in mind, our study yields valuable insight into past and current measles dynamics in a previously understudied subpopulation.

In summary, we have provided the most detailed $R_0$ and reporting rate $\rho$ estimates for within school and age classes based on time-series outbreak data. These estimates confirm beliefs that high city-level $R_0$ estimates are driven by school-aged children. Applying these results to the postvaccine landscape demonstrates the need for increased vaccine uptake in school-aged children in certain California schools.

**Broader Implications and Future Work**

Our results underpin a number of implications for cross-scale dynamics in human–environment interactions. First, we have demonstrated major hotspots of infection at the school level, even despite still relatively smooth “predator–prey” oscillations at the city level (1). This implies “emergent simplicity,” despite many complexities at finer scales (Fig. 1). To dissect this contradiction, we need to construct network models and the associated approximations spanning the underlying family-school-population level (Fig. 1). However, to take this analysis further, the key need here (as in all cross-scale dynamics) is acquiring data that record dynamics at the relevant intermediate scales. This paper is a first step for schools. An important area of future development includes the construction and analysis of community-wide network models that may further reconcile the coarse- with the fine-grain dynamics.

**Materials and Methods**

The Dataset and Inclusion Criteria. To obtain prevaccination era school data we searched the Wellcome Library online archives collection “London’s Pulse: Medical Officer of Health Reports 1848–1972” (33). We found two records of interest. First, the “Annual Report of the Medical Officer of Health for Woolwich, 1904” provides an appendix (ref. 34, appendix I, p. 129) on the incidence of measles in classes, Christmas to May 1904, in 18 elementary schools of the borough of Woolwich, London. Second, the “Report of the Medical Officer of Health for London County Council, 1904” gives an appendix (ref. 35, p. 46) with detailed accounts of outbreaks of measles in 15 elementary schools of the borough of Woolwich in 1904 that partially overlaps with the Woolwich report. This report provides qualitative information on the mode of transmission between children in school versus out of school. Additionally, the documentation provides information on transmission during classes and holiday, as well as the efficiency of measures taken by school teachers to stop the spread of the measles. Both datasets reported that no students died of measles. Although daily data are reported, we use weekly incidence for our analysis because weekends serve as a natural weekly clock. In our study we break our data into two sets: (i) school data and (ii) epidemics disaggregated by school and class.

Because our time series contain multiple peaks as well as large variability in the number of reported cases, we devise selection criteria to determine which time series are suitable for statistical inference. We use two criteria: (i) the total number of cases must be greater than eight and (ii) the time series must pass the Ljung–Box test; this is a portmanteau test that looks at the overall randomness based on a set number of lags in the data. Because we assume a Markov process, we take the number of lags to be a single time step $\Delta t = 1$ week. The Ljung–Box test assumes the null hypothesis that the data are independently distributed, thus any observed correlation is from random sampling, and the alternative hypothesis is that the data are not independently distributed (36). To reject the null hypothesis, we adopt a $P$ value less than 0.05. In Fig. 6 we show our selection criteria for the schools dataset as well as an example of a dataset we select (Bloomfield Road). We emphasize the behavior of a simple, closed SIR model, and a dataset we reject (Union Street) due to minimal cases and a more complicated epidemic pattern. Many time series have a number of zeros before the outbreak begins, so we take our start time, $t_0$, for inference to be the first week in which we have nonzero cases, and then set our initial condition $S_0 = C(t_0)$, where $C$ is the observed cases. Additionally, the Vicarage Road School time series is characterized by two outbreaks with 14 wk between them, indicating two completely separate events. Because the SIR with constant contact assumes a single outbreak, we only use the second outbreak to infer parameters. The first outbreak has a peak size of 9, and the second 21. We note that in Fig. 6 we have two relative outliers, Purrett Road and Eglington Road, which we address in Supporting Information.

The school sizes range between 403 and 1,631 students aged 3 to 8 y. Additionally, we have record card data for each school and class that allow us to estimate how many students previously had measles and were thus immune. Because these only represent a sample of each class size, we linearly interpolate these susceptible and recovered ratios to the whole school or class to use as our initial conditions. At the school level, average susceptibility is 45%, whereas average by age susceptibility is 53%. These percentages are calculated using an average of the time series that pass our selection criteria. The difference between these two is likely attributed to a number of the older classes, ages 7 and 8 y, having zero cases and lower susceptibility. A box plot of this difference is seen in Fig. 2A.

To obtain recent school vaccination rates we used and summarized reports of MMR vaccine and exemption status in California kindergartens reported by California Department of Public Health (2015–2016) (25). Although there is some evidence that vaccine status may be underestimated (30), the current vaccine landscape still falls below the critical vaccination threshold in particular locales. All datasets are freely available online (25, 33–35). Additionally, the school data used have been archived (https://github.com/adbecker/1904WoolwichMeasles).

**Epidemic Models and Inference.** Within the school year, we assume a simple mass-action epidemic (4) with no recruitment into the susceptible class. In this setting, the assumptions of frequency and density dependence give rise to similar dynamics given the small group size and high transmission rate (37). We use a continuous time model under the assumption that the epidemic is a partially observed Markov process. Using a stochastic SIR model with constant contact during the school term, the probability of success of an infection is modeled as a dispersed negative binomial to allow for underreporting, $\psi$, and measurement error, $\nu$ (ref. 38). Mathematically this is equivalent to $C \sim NB(\nu \times Incidence, \psi^2)$. The parameter $\psi$ can be seen as the shape parameter for an overdispersed Poisson distribution (38). We choose an SIR model over an SEIR (susceptible, exposed,