THE THERMAL CLASSIFICATION OF LAKES*

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Forell1 introduced, for holomictic lakes of sufficient depth to exhibit thermal stratification, a threefold classification in which the following categories were recognized: polar lakes, never at any point over 4° C., inversely stratified under ice in winter and circulating in summer; temperate lakes, inversely stratified in winter, directly stratified in summer, and circulating twice a year at about 4° C.; and tropical lakes, always at every point above 4° C., circulating in winter and directly stratified in summer.

The terminology has been long considered inappropriate, as many of the finest examples of Forell’s tropical type occur in western Scotland and in British Columbia, regions far outside the tropics, while, of the few polar lakes studied, more occur at high altitudes in temperate and tropical latitudes than within the Arctic Circle. It has also become apparent, since the magnificent work of Ruttner2 in Indonesia, that the typical lake of the humid tropics at low altitudes circulates rarely, in an irregular manner, not at a specific season but when exceptional periods of cool weather permit sufficient heat loss at the surface to cause instability. This presumably happens at intervals of length greater than that of a year.

Recently one of us (H. L.) has had the opportunity to study lakes in equatorial latitudes but at great altitudes, in the Andes. Although at low altitudes in the humid tropics small temperature gradients can maintain stable stratifications, no stable stratification develops at the low temperatures of high altitudes, where the density difference per degree centigrade is very small. The lack of seasonal variation, that permits almost perennial stratification at low altitudes in equatorial latitudes, thus permits perennial circulation at high altitudes in the same latitudes.

We propose for these two types of equatorial lake the terms oligomictic and polymictic, respectively. For the three categories of Forell’s classification the terms cold monomictic, dimictic, and warm monomictic have been used by one of us (G. E. H.) in a forthcoming extensive work on limnology.3 The theoretical scheme (Fig. 1) may be completed by recognizing for the very rare perennially ice-covered

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6 D. W. Barton, Cytologia, 19, 157–175, 1954.
8 A. Hannah, Advances in Genet., 4, 87–121, 1951.
lakes of the Antarctic and, under special conditions, of some high mountains (Löfler unpublished) a category of amictic lakes, perennally sealed off by ice from most of the annual seasonal variations in temperature.4

It is evident from the considerable body of work on Central Africa that in the dry equatorial regions of that continent at fair elevations a great variety of conditions occur, linking the oligomictic, with a strong tendency to meromixsis, as in Lake Nyasa,6 the warm monomictic, as in Lake Mohasi, Ruanda,6 and the polymictic, as in Lake Tana,7 Lake Rudolf, Lake Albert, and, to a large extent, Lake Victoria and Lake Naivasha.8 The existence of special climatic regimes, notably the
monsoonal regime of India and Ceylon, probably produces considerable disturbance of the scheme; Dr. S. Dillon Ripley, for instance, tells us that in Ceylon artificial lakes at an altitude slightly over 2,000 meters may occasionally freeze, though such lakes are certainly not polymictic and presumably belong in the dimictic category.

Further details will be found in our forthcoming independent works.

* This paper is dedicated to Professor Alexander Petrunkevitch on his eightieth birthday. Contribution from the Osborn Zoological Laboratory, Yale University, New Haven, Connecticut.
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* G. Morandini, Missione di studio al Lago Tana, Vol. 3: Ricerche limnologiche, Part 1, "Geografia-fisica" (Rome, 1940). This author completes the Forellian scheme by the addition of an equatorial type for the freely circulating lakes of the tropics. It is, however, apparent that two extreme types occur in equatorial latitudes, depending on the altitude, as is indicated in the present note.


\[ \frac{\Delta(s)}{\mu(x)^s} = \int_{p} e^{-\lambda(t)x} R(t)^s d\Omega(t), \]

which each time, by an appropriate computation, turns out to be a product

\[ \prod_{m=1}^{N} \Gamma(p_m s + q_m), \]

in which \( p_m \) are positive rational numbers and \( q_m \) are complex numbers.\(^1\) After replacing \( \Delta(s) \) by \( \Delta(r \alpha) \) for a suitable positive integer \( r \), the numbers \( p_m \) may be assumed to be positive integers themselves, and, applying, now, the classical

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**Gamma Factors in Functional Equations**

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In a so-called "functional" equation for a zeta function pertaining to an algebraic field or a modular setup, the Dirichlet series occurring is multiplied by a function \( \Delta(s) \) of the complex variable \( s = \sigma + i \tau \) which introduces itself each time by some (multiple Euler) integral of the form

\[ \frac{\Delta(s)}{\mu(x)^s} = \int_{p} e^{-\lambda(t)x} R(t)^s d\Omega(t), \]