

Saturation wind power potential and its implications for wind energy

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Wind turbines convert kinetic to electrical energy, which returns to the atmosphere as heat to regenerate some potential and kinetic energy. As the number of wind turbines increases over large geographic regions, power extraction first increases linearly, but then converges to a saturation potential not identified previously from physical principles or turbine properties. These saturation potentials are >250 terawatts (TW) at 100 m globally, approximately 80 TW at 100 m over land plus coastal ocean outside Antarctica, and approximately 380 TW at 10 km in the jet streams. Thus, there is no fundamental barrier to obtaining half (approximately 5.75 TW) or several times the world's all-purpose power from wind in a 2030 clean-energy economy.

atmospheric modeling | climate feedbacks | renewable energy | water vapor | clean energy economy

A new method is proposed to determine the maximum theoretical wind power potential on Earth, based on the concept of “saturation”. The *saturation wind power potential* (SWPP) is the maximum wind power that can be extracted upon increasing the number of wind turbines over a large geographic region, independent of societal, environmental, climatic, or economic considerations. Once the SWPP is reached, increasing the number of turbines further does not increase the generated power further. At the SWPP, winds still occur because individual turbines can extract no more than 59.3 % of the kinetic energy in the wind (Betz's limit). This paper also defines the *fixed wind power potential* (FWPP), which is the maximum power that can be extracted by a fixed number of wind turbines at decreasing installed density and increasing geographic area. The SWPP is calculated here at 100 m above ground, the hub height of most modern wind turbines, assuming conventional wind turbines distributed everywhere on Earth, including over the oceans (simulation named “global-SWPP”) and, separately, over land only but excluding Antarctica (“land-SWPP”). The SWPP is also calculated at 10 km above ground in the jet streams assuming airborne wind energy devices (“jet stream-SWPP”). Capturing jet stream winds presents greater technological challenges than capturing surface winds but is still of interest (1, 2).

The main purpose of these simulations is to use a physical model to determine the theoretical limit of wind energy available at these altitudes, particularly because some recent studies that accounted for energy extraction by turbines, but not physically, have suggested that available wind energy is small (2, 3). Previous theoretical estimates of the power in the wind (4–9) are similarly not based on a physical model of energy extraction so cannot give estimates of wind potential at the height of turbines. As found here, energy extraction at a given altitude does not deplete energy at all altitudes above or below it; so an estimate of wind potential in the whole atmosphere does not answer the practical question about wind turbine potential at typical hub heights.

More relevant for practical applications, the FWPP of four million turbines at 100 m in three different configurations is quantified here to determine if this number is sufficient for powering half the world's all-purpose power demand in a 2030 clean-energy economy (10).

It is well known that the array efficiency of a single wind or water farm containing many turbines decreases with decreasing distance between turbines (11, 12). However, what is not known is the extent to which the efficiency loss operates globally when realistic meteorology and energy extraction by turbines are accounted for. This information is critical for determining the feasibility of a worldwide renewable energy future. Calculating the SWPP for large penetrations of wind (≥ 1 TW) is not currently possible from data analysis, because penetrations are still low (239 gigawatts (GW) installed worldwide at the start of 2012). The most accurate method available to analyze this issue is with a complex 3D atmospheric-ocean-land coupled model.

Previous global simulations of wind farms have assumed that wind farm effects on the atmosphere can be represented by changing surface roughness or adding a drag coefficient (2, 13–17). Roughness parameterizations, though, incorrectly reduce wind speeds the most in the bottom model layer, whereas in reality a surface wind turbine reduces wind speed the most at hub height, approximately 100 m above ground (Fig. 1). Because roughness lengths and drag coefficients are approximate, it is also difficult to ensure they extract the correct amount of energy from the wind. Calaf, et al. (18) demonstrated the inaccuracy of standard roughness parameterizations against large-eddy simulation results and developed a multiple layer roughness parameterization for ground-based turbines that is more accurate. Here, however, we use a straightforward approach to calculate the momentum sink at any specified hub height, not just near the ground, but also aloft, each time step, because it precisely determines the time-dependent energy extraction from one or many turbines.

Another common omission during modeling has been that of energy conservation during electric power use and turbulence dissipation. If wind turbines generate 5.75 TW (0.0113 W/m^2), such power ultimately returns to the air as heat following electricity use. This heat does not depend on the electricity source, thus it is also released when coal, nuclear, and natural gas produce electricity. Such generators, though, produce additional heat due to combustion or nuclear reaction and emit global warming pollutants (10, 19). As such, wind turbines reduce direct heat and pollutant emissions compared with conventional generators. However, the electricity use still needs to be accounted for because the heat is a source of some regenerated kinetic energy (via conversion of internal energy to some available potential energy to kinetic energy). To date, only ref. 1 has calculated the heat from electricity returned to the air, but they focused on airborne rather than ground-based wind turbines.

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speed and small turbulence change near the surface due to turbines contributed in the model to reducing surface evaporation. Uncertainties in the treatment of turbulence still exist due to both the coarse horizontal resolution of the model and the simplification of no turbine-rotor generated turbulence.

Reduced evaporation reduced evaporative cooling of the surface, first warming the surface. However, because evaporated water vapor normally recondenses in the atmosphere to form clouds, releasing latent heat there, the reduction in water vapor reduced latent heat release in the air, cooling the air due as a result of this process. Because water vapor contributes to air pressure, reducing water vapor also reduced globally averaged air pressure by approximately 0.3 and approximately 0.1 hPa in the global (Simulation B) and land (I) cases, respectively. Because water vapor is a greenhouse gas, reducing it increased thermal-IR radiation escape to space, cooling the surface further. However, less water also reduced cloudiness, increasing solar radiation to the surface during the day but increasing outgoing thermal-IR at night, thus causing a slight warming at night, as observed (27, 30). The net effect of all five changes (air cooling due to lower atmospheric latent heat release, ground warming due to lower surface water evaporation, air and ground cooling due to a reduced water vapor greenhouse effect, ground warming due to reduced daytime cloudiness, and ground cooling due to reduced nighttime cloudiness) was a globally averaged surface-air temperature decrease in 15 out of the 16 surface-turbine simulations. This result is expected because water vapor is known to cause net warming of the atmosphere, so reducing it should cause cooling (31). Temperature results, though, are still uncertain, particularly due to the uncertainty of clouds and the transient nature of the simulations and could change over longer simulations because full temperature responses take decades to realize. A certain benefit of the slower winds, though, is the reduction in wind-driven soil dust; sea spray; and spore, pollen, and bacteria emissions, reducing human exposure to small particles that penetrate deep into the lungs.

Globally distributed turbines decreased zonal winds; however, they increased meridional winds in the pole-ward direction in both hemispheres (Fig. S4 A and B). The pole-ward transport of air increased the pressure gradient between the poles and Equator by approximately 15–25 hPa, supporting the contention that the atmosphere responded to the increased dissipation of kinetic energy by increasing some of its available potential energy via enhanced pole-to-Equator pressure gradients. Reduced water vapor partial pressure at low latitudes contributed slightly to the enhanced pressure gradient.

Global warming increases temperatures at the poles more than lower latitudes. The temperature gradient reduction could reduce global near-surface wind resources in the future although ocean wind resources over the last 25 years have increased in the global average according to multiple datasets (32). Higher water vapor due to future warming will also likely offset reduced water vapor due to wind turbines.

Jet-stream turbines reduced mean wind speeds at altitudes above and below them, but increased boundary-layer wind speeds (Fig. 1C). Like in the surface case, turbines decreased zonal wind speeds substantially (Fig. S5A), but increased meridional wind speeds (Fig. S5B), moving air pole-ward at 10 km but equator-ward near the surface in both hemispheres, following the respective pressure gradients (Fig. S5C). Lower surface pressure in the tropics through midlatitudes caused air to rise, expand, and cool adiabatically, decreasing temperatures at all altitudes (Fig. S5D) and increasing both cloud liquid below 5 km (Fig. S5E) and cloud ice above that. Enhanced cloudiness increased precipitation, and both, together with net divergence, decreased water vapor in the tropics and subtropics and increased it toward the poles (Fig. S5F). Compressional heating over the poles increased temperatures there, but the net effect of jet stream turbines was surface cooling by >1 K (Fig. S5F), as cold air advection from the Poles prevailed near the surface. Interestingly, the higher boundary-layer wind speeds (Fig. 1C and Fig. S5A) increased evaporation there, but enhanced condensation of that vapor decreased column vapor at low latitudes (Fig. S5F).

In sum, increasing the number of wind turbines worldwide allows energy extraction relatively proportional to the number of turbines until saturation is reached. Saturation occurs when sources of kinetic energy at nearby altitudes and creation of kinetic from potential energy are exhausted. At saturation, each additional turbine still extracts energy, but that extraction reduces energy available to other turbines, so the average extraction among all turbines decreases to maintain a constant SWPP. The results here suggest that saturation of wind power availability will not limit a clean-energy economy. However, spreading wind farms out worldwide in high-wind locations will increase wind farm efficiency and reduce the number of farms needed compared with packing wind farms side-by-side. The careful siting of wind farms will minimize costs and the overall impacts of a global wind infrastructure on the environment.

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- Archer CL, Caldeira K (2009) Global assessment of high-altitude wind power. *Energies* 2:307–319.
- Miller LM, Gans F, Kleidon A (2011) Jet stream wind power as a renewable energy resource: Little power, big impacts. *Earth Syst Dynam* 2:201–212.
- De Castro C, Mediavilla M, Miguel LJ, Frechoso F (2011) Global wind power potential and technological limits. *Energy Policy* 39:6677–6682.
- Lorenz EN (1967) *The Nature and Theory of the General Circulation of the Atmosphere* (WMO, Geneva) p 161.
- Gustavson MR (1979) Limits to wind power utilization. *Science* 204:13–17.
- Peixoto JP, Oort AH (1992) *Physics of Climate* (American Institute of Physics, New York) p 520.
- Sorensen B (2004) *Renewable Energy: Its Physics, Engineering, Use, Environmental Impacts, Economy, and Planning Aspects* (Elsevier Academic Press, London), 3rd Ed, p 86.
- Li L, Ingersoll AP, Jiang X, Feldman D, Yung YL (2007) Lorenz energy cycle of the global atmosphere based on reanalysis datasets. *Geophys Res Lett* 34:L16813.
- Stacey FD, Davis PM (2008) *Physics of the Earth* (Cambridge Univ Press, Cambridge), 4th Ed, p 531.
- Jacobson MZ, Delucchi MA (2011) Providing all global energy with wind, water, and solar power, part I: Technologies, energy resources, quantities and areas of infrastructure, and materials. *Energy Policy* 39:1154–1169.
- Milborrow DJ (1980) The performance of arrays of wind turbines. *J Wind Eng Ind Aerod* 5:403–430.
- Li Y, Calisal SM (2010) Estimating power output from a tidal current turbine farm with first-order approximation of hydrodynamic interaction between turbines. *Int J Green Energy* 7:153–163.
- Keith DW, et al. (2004) The influence of large-scale wind power on global climate. *Proc Natl Acad Sci USA* 101:16115–16120.
- Kirk-Davidoff DB, Keith D (2008) On the climate impact of surface roughness anomalies. *J Atmos Sci* 65:2215–2234.
- Barrie D, Kirk-Davidoff DB (2010) Weather response to a large wind turbine array. *Atmos Chem Phys* 10:769–775.
- Wang C, Prinn RJ (2010) Potential climatic impacts and reliability of very large-scale wind farms. *Atmos Chem Phys* 10:2053–2061.
- Miller LM, Gans F, Kleidon A (2011) Estimating maximum global land surface wind power extractability and associated climatic consequences. *Earth Syst Dynam* 2:1–12.
- Calaf M, Meneyeau C, Meyers J (2010) Large eddy simulation study of fully developed wind-turbine array boundary layers. *Phys Fluids* 22:015110.
- Sta Maria MRV, Jacobson MZ (2009) Investigating the effect of large wind farms on energy in the atmosphere. *Energies* 2:816–836.
- Jacobson MZ, Wilkerson JT, Naiman AD, Lele SK (2011) The effects of aircraft on climate and pollution. Part I: Numerical methods for treating the subgrid evolution of discrete size- and composition-resolved contrails from all commercial flights worldwide. *J Comp Phys* 230:5115–5132.
- Jacobson MZ, Ten Hoeve JE (2012) Effects of urban surfaces and white roofs on global and regional climate. *J Climate* 25:1028–1044.
- Baidya Roy S, Pacala SW, Walko RI (2004) Can large wind farms affect local meteorology. *J Geophys Res* 109:D19101.
- Baidya Roy S (2011) Simulating impacts of wind farms on local hydrometeorology. *J Wind Eng Ind Aerod* 99:491–498.

24. Pryor SC, Nikulin G, Jones C (2012) Assessing climate change impacts on the near-term stability of the wind energy resources over the United States. *J Geophys Res* 117:D03117.
25. Lu X, McElroy M, Kiviluoma J (2009) Global potential for wind-generated electricity. *Proc Natl Acad Sci USA* 106:10933–10938.
26. Archer CL, Jacobson MZ (2005) Evaluation of global wind power. *J Geophys Res* 110:D12110.
27. Zhou L, et al. (2012) Impacts of wind farms on land surface temperatures. *Nature Climate Change* 2:539–543.
28. Vermeer LJ, Sorensen JN, Crespo A (2003) Wind turbine wake aerodynamics. *Progr Aero Sci* 39:467–510.
29. Crespo A, Hernandez J (1996) Turbulence characteristics in wind-turbine wakes. *J Wind Eng Ind Aerod* 61:71–85.
30. Baidya Roy S, Traiteur JJ (2010) Impacts of wind farms on surface air temperatures. *Proc Natl Acad Sci USA* 107:17899–17904.
31. Kiehl JT, Trenberth KE (1997) Earth's annual global mean energy budget. *Bull Am Meteorol Soc* 78:197–208.
32. Wentz FJ, Ricciardulli L (2011) Comment on "Global trends in wind speed and wave height". *Science* 334:905.
33. Lettau H (1969) Note on aerodynamic roughness-parameter estimation on the basis of roughness-element description. *J Appl Meteorol* 8:828–832.