

Quantum erasure with causally disconnected choice

Xiao-Song Ma^{a,b,1,2}, Johannes Kofler^{a,3}, Angie Qarry^{a,b}, Nuray Tetik^{a,b}, Thomas Scheidl^a, Rupert Ursin^a, Sven Ramelow^{a,b}, Thomas Herbst^{a,b}, Lothar Ratschbacher^{a,b,4}, Alessandro Fedrizzi^{a,b,5}, Thomas Jennewein^{a,6}, and Anton Zeilinger^{a,b,1}

^aInstitute for Quantum Optics and Quantum Information, Austrian Academy of Sciences, A-1090 Vienna, Austria; and ^bVienna Center for Quantum Science and Technology, Faculty of Physics, University of Vienna, Boltzmanngasse 5, A-1090 Vienna, Austria

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The counterintuitive features of quantum physics challenge many common-sense assumptions. In an interferometric quantum eraser experiment, one can actively choose whether or not to erase which-path information (a particle feature) of one quantum system and thus observe its wave feature via interference or not by performing a suitable measurement on a distant quantum system entangled with it. In all experiments performed to date, this choice took place either in the past or, in some delayed-choice arrangements, in the future of the interference. Thus, in principle, physical communications between choice and interference were not excluded. Here, we report a quantum eraser experiment in which, by enforcing Einstein locality, no such communication is possible. This is achieved by independent active choices, which are space-like separated from the interference. Our setup employs hybrid path-polarization entangled photon pairs, which are distributed over an optical fiber link of 55 m in one experiment, or over a free-space link of 144 km in another. No naive realistic picture is compatible with our results because whether a quantum could be seen as showing particle- or wave-like behavior would depend on a causally disconnected choice. It is therefore suggestive to abandon such pictures altogether.

quantum foundations | quantum optics | quantum information processing

Wave-particle duality is a well-known manifestation of the more general complementarity principle in quantum physics (1). Several single-photon experiments (2–6) confirmed both the wave and the particle nature of light. Another manifestation of complementarity is that the position and linear momentum of individual particles cannot be well-defined together as highlighted in Heisenberg's uncertainty relation (7). Based on the concept of the Heisenberg microscope (7), von Weizsäcker (8, 9) discussed the gedanken experiment in which a photon interacts with an electron. In today's language, after the interaction the photon and the electron are in an entangled state (10, 11) in which their positions and momenta are strongly correlated. Therefore, different complementary measurements on the photon allow choosing whether the electron acquires a well-defined position or a well-defined momentum. According to Bohr, "it obviously can make no difference as regards observable effects [...] whether our plans of constructing or handling the instruments are fixed beforehand or whether we prefer to postpone the completion of our planning until a later moment [...]" (p 230, ref. 1).

Wheeler later proposed an experiment on wave-particle duality in which the paths of a single photon, coming from a distant star, form a very large interferometer (12, 13). Inserting or not inserting a beam splitter at the end of the interferometer's paths will allow one to either observe interference (wave behavior) or acquire path information (particle behavior), respectively. Wheeler proposed to delay the choice of whether or not to insert the beam splitter until the very last moment of the photon's travel inside the interferometer. This rules out the possibility that the photon knew the configuration beforehand and adapted its behavior accordingly (*, 14). He then pointed out the seemingly paradoxical situation that it depends on the experimenter's delayed choice whether the photon behaved as a particle or

a wave. In Wheeler's words: "We, now, by moving the mirror in or out have an unavoidable effect on what we have a right to say about the *already* past history of that photon" (13). Since then, Wheeler's proposal has led to several experimental studies with single-photon interference (†, ‡, 15–19), which provided increasingly sophisticated demonstrations of the wave-particle duality of single quanta, even in a delayed-choice configuration.

Scully and Drühl proposed the so-called quantum eraser (20), in which maximally entangled atom-photon states were studied. In ref. 21, the atoms, which can be interpreted as the "system," are sent through a double slit. Each atom spontaneously emits a photon, which can be regarded as the "environment," carrying *welcher-weg* (which-path) information on which of the two slits the atom takes. No interference pattern of atoms will be obtainable after the double slit, if one ignores the presence of the photons, because every photon carries the *welcher-weg* information about the corresponding atom. The presence of path information anywhere in the universe is sufficient to prohibit any possibility of interference. It is irrelevant whether a future observer might decide to acquire it. The mere possibility is enough. In other words, the atoms' path states alone are not in a coherent superposition due to the atom-photon entanglement.

If the observer measures the photons, his choice of the type of measurement decides whether the atoms can be described by

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¹To whom correspondence may be addressed. E-mail: xiaosong.ma@univie.ac.at or Anton.Zeilinger@univie.ac.at.

²Present address: Department of Electrical Engineering, Yale University, New Haven, CT 06520.

³Present address: Max Planck Institute of Quantum Optics, 85748 Garching/Munich, Germany.

⁴Present address: Cavendish Laboratory, University of Cambridge, Cambridge CB3 0HE, United Kingdom.

⁵Present address: Centre for Engineered Quantum Systems and Centre for Quantum Computer and Communication Technology, School of Mathematics and Physics, University of Queensland, Brisbane 4072, Australia.

⁶Present address: Institute for Quantum Computing and Department of Physics and Astronomy, University of Waterloo, Waterloo, ON, Canada N2L 3G1.

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*Mittelstaedt P (1987) Proceedings of the Second International Symposium on Foundations of Quantum Mechanics, September 1–4, 1986, Tokyo, Japan, eds Namiki M, Ohnuki Y, Murayama Y, Nomura S (Physics Society of Japan, Tokyo), pp 53–58.

†Hellmuth T, Zajonc AG, Walther H (1985) Symposium on Foundations of Modern Physics, June 16–20, 1985, Joensuu, Finland, eds Lahti P, Mittelstaedt P (World Scientific, Singapore), pp 417–421.

‡Alley CO, Jacobowicz OG, Wickes WC (1987) Proceedings of the Second International Symposium on the Foundations of Quantum Mechanics, September 1–4, 1986, Tokyo, Japan, ed Narani H (Physics Society of Japan, Tokyo), pp 36–47.

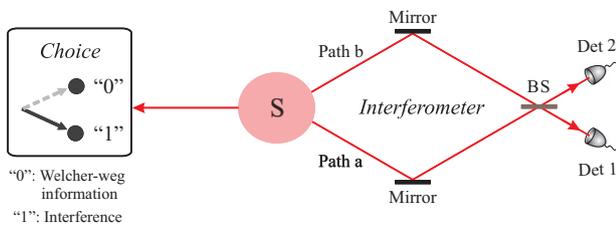


Fig. 1. Concept of our quantum eraser under Einstein locality conditions. Hybrid entangled photon-pair source, labeled as S, emits path-polarization entangled photon pairs. System photons are propagating through an interferometer (Right) and the environment photons are subject to polarization measurements (Left). Choices to acquire *welcher-weg* information or to obtain interference of the system photons are made under Einstein locality so that there are no causal influences between the system photons and the environment photons.

a wave or a particle picture. First, when the photons are measured in a way that reveals *welcher-weg* information of the atoms, the atoms do not show interference, not even conditionally on the photons' specific measurement results. Second, if the photons are measured such that this irrevocably erases any *welcher-weg* information about the atoms, then the atoms will show

perfect but distinct interference patterns, which are each other's complement and are conditioned on the specific outcomes of the photons' measurements. These two scenarios illustrate a further manifestation of the complementarity principle, in addition to the wave-particle duality. There is a tradeoff between acquiring the atoms' path information or their interference pattern via complementary measurements on the photons and not on the atoms themselves. A continuous transition between these two extreme situations exists, where partial *welcher-weg* information and interference patterns with reduced visibility can be obtained (22, 23).

The authors of refs. 20 and 21 proposed to combine the delayed-choice paradigm with the quantum eraser concept. Because the *welcher-weg* information of the atoms is carried by the photons, the choice of measurement of the photons—either revealing or erasing the atoms' *welcher-weg* information—can be delayed until “long after the atoms have passed” the photon detectors at the double slit (p 114, 21). The later measurement of the photons “decides” whether the atoms can show interference or not, even after the atoms have been detected. This seemingly counterintuitive situation comes from the fact that in a bipartite quantum state the observed correlations are independent of the space-time arrangement of the measurements on the individual systems. Thereby, their proposed scheme significantly extended the concept of the single-photon delayed-

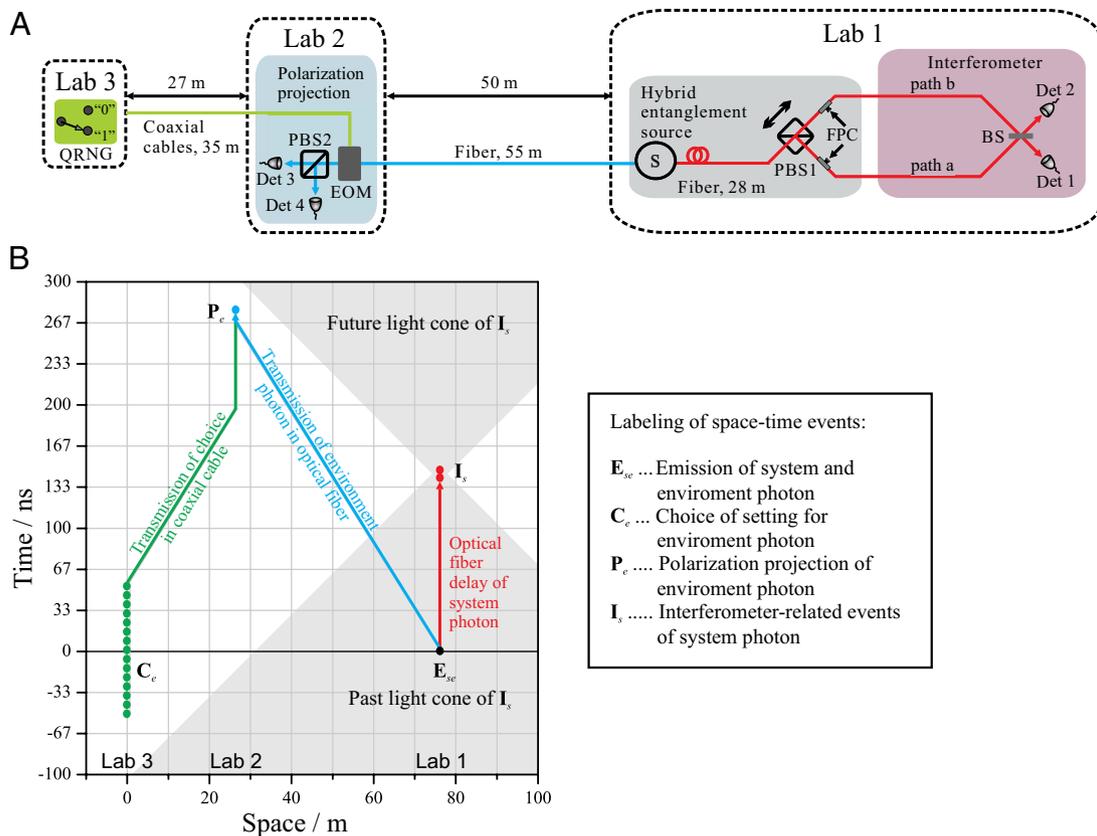


Fig. 2. (A) Scheme of the Vienna experiment: In Lab 1, the source (S) emits polarization entangled photon pairs, each consisting of a system and an environment photon, via type-II spontaneous parametric down-conversion. Good spectral and spatial mode overlap is achieved by using interference filters with 1-nm bandwidth and by collecting the photons into single-mode fibers. The polarization entangled state is subsequently converted into a hybrid entangled state with a polarizing beam splitter (PBS1) and two fiber polarization controllers (FPC). Interferometric measurement of the system photon is performed with a single-mode fiber beam splitter (BS) with a path length of 2 m, where the relative phase between path a and path b is adjusted by moving PBS1's position with a piezo-nanopositioner. The polarization projection setup of the environment photon consists of an electro-optic modulator (EOM) and another PBS (PBS2). Both photons are detected by silicon avalanche photodiodes (DET 1–4). The choice is made with a QRNG (44). (B) Space-time diagram. The choice-related events C_e and the polarization projection of the environment photon P_e are space-like separated from all events of the interferometric measurement of the system photon I_s . Additionally, the events C_e are also space-like separated from the emission of the entangled photon pair from the source E_{se} . Shaded areas are the past and the future light cones of events I_s . This ensures that Einstein locality is fulfilled. Details are provided in the main text and *SI Text*. BS, beam splitter; FPCs, fiber polarization controllers; PBS, polarized beam splitter.

Our work demonstrates and confirms that whether the correlations between two entangled photons reveal *welcher-weg* information or an interference pattern of one (system) photon depends on the choice of measurement on the other (environment) photon, even when all of the events on the two sides that can be space-like separated are space-like separated. The fact that it is possible to decide whether a wave or particle feature manifests itself long after—and even space-like separated from—the measurement teaches us that we should not have any naive realistic picture for interpreting quantum phenomena. Any explanation of what goes on in a specific individual observation of one photon has to take into account the whole experimental apparatus of the complete quantum state consisting of both photons, and it can only make sense after all information concerning complementary variables has been recorded. Our results demonstrate that the viewpoint that the system photon behaves either definitely as a wave or definitely as

a particle would require faster-than-light communication. Because this would be in strong tension with the special theory of relativity, we believe that such a viewpoint should be given up entirely.

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- Bohr N (1949) Discussion with Einstein on epistemological problems in atomic physics. *Albert Einstein: Philosopher-Scientist VII*, ed Schilpp PA (Library of Living Philosophers, Evanston, IL), Vol 7, pp 201–241.
- Clauser JF (1949) Experimental distinction between the quantum and classical field-theoretic predictions for the photoelectric effect. *Phys Rev D* 9:853–860.
- Grangier P, Roger G, Aspect A (1986) Experimental evidence for a photon anticorrelation effect on a beam splitter: A new light on single-photon interferences. *Europhys Lett* 1:173–179.
- Dopfer B (1998) Zwei Experimente zur Interferenz von Zwei-Photon Zuständen: Ein Heisenbergmikroskop und Pendellösung. PhD Thesis (University of Innsbruck, Innsbruck, Austria). German.
- Zeilinger A (2000) Experiment and the foundations of quantum physics. *Rev Mod Phys* 71:S288–S297.
- Zeilinger A, Weihs G, Jennewein T, Aspelmeyer M (2005) Happy centenary, photon. *Nature* 433(7023):230–238.
- Heisenberg W (1927) Über den anschaulichen Inhalt der quantentheoretischen Kinematik und Mechanik. *Z Phys* 43:172–198. German.
- von Weizsäcker CF (1931) Ortsbestimmung eines Elektrons durch ein Mikroskop. *Z Phys* 70:114–130. German.
- von Weizsäcker CF (1941) Zur Deutung der Quantenmechanik. *Z Phys* 118:489–509. German.
- Einstein A, Podolsky B, Rosen N (1935) Can quantum mechanical description of physical reality be considered complete? *Phys Rev* 47:777–780.
- Schrödinger E (1935) Die gegenwärtige Situation in der Quantenmechanik. *Naturwiss* 23:807–812, 823–828, 844–849; trans Wheeler JA, Zurek WH (1980) *Proc Am Philos Soc* (Princeton Univ Press), 124, 323–338. German.
- Wheeler JA (1978) The “past” and the “delayed-choice” double-slit experiment. *Mathematical Foundations of Quantum Theory* (Academic, New York), pp 9–48.
- Wheeler JA (1984) Law without law. *Quantum Theory and Measurement* (Princeton Univ Press, Princeton), pp 182–213.
- Greenstein G, Zajonc AG (2005) *The Quantum Challenge* (Jones and Bartlett, Boston), 2nd Ed.
- Hellmuth T, Walther H, Zajonc AG, Schleich W (1987) Delayed-choice experiments in quantum interference. *Phys Rev A* 35(6):2532–2541.
- Baldzuhn J, Mohler E, Martienssen W (1989) A wave-particle delayed-choice experiment with a single-photon state. *Z Phys B: Condens Matter* 77:347–352.
- Lawson-Daku BJ, et al. (1996) Delayed choices in atom Stern-Gerlach interferometry. *Phys Rev A* 54(6):5042–5047.
- Jacques V, et al. (2007) Experimental realization of Wheeler’s delayed-choice Gedanken experiment. *Science* 315(5814):966–968.
- Jacques V, et al. (2008) Delayed-choice test of quantum complementarity with interfering single photons. *Phys Rev Lett* 100(22):220402.
- Scully MO, Drühl K (1982) Quantum eraser: A proposed photon correlation experiment concerning observation and “delayed choice” in quantum mechanics. *Phys Rev A* 25:2208–2213.
- Scully MO, Englert BG, Walther H (1991) Quantum optical tests of complementarity. *Nature* 351:111–116.
- Wooters WK, Zurek WH (1979) Complementarity in the double-slit experiment: Quantum nonseparability and a quantitative statement of Bohr’s principle. *Phys Rev D Part Fields* 19:473–484.
- Mittelstaedt P, Prieur A, Schieder R (1987) Unsharp particle-wave duality in a photon slit-beam experiment. *Found Phys* 17:891–903.
- Englert BG, Bergou JA (2000) Quantitative quantum erasure. *Opt Commun* 179:337–355.
- Kwiat PG, Englert BG (2004) *Science and Ultimate Reality: Quantum Theory, Cosmology and Complexity*, eds Barrow JD, Davies PCW, Charles J, Harper L (Cambridge Univ Press, Cambridge).
- Aharonov Y, Zurek WH (2005) Time and the quantum: Erasing the past and impacting the future. *Science* 307(5711):875–879.
- Eichmann U, et al. (1993) Young’s interference experiment with light scattered from two atoms. *Phys Rev Lett* 70(16):2359–2362.
- Kim YH, Yu R, Kulik SP, Shih Y, Scully MO (2000) Delayed “choice” quantum eraser. *Phys Rev Lett* 84(1):1–5.
- Walborn SP, Terra Cunha MO, Pádua S, Monken CH (2002) Double-slit quantum eraser. *Phys Rev A* 65:033818.
- Peres A (2000) Delayed choice for entanglement swapping. *J Mod Opt* 47:139–143.
- Jennewein T, Weihs G, Pan JW, Zeilinger A (2002) Experimental nonlocality proof of quantum teleportation and entanglement swapping. *Phys Rev Lett* 88(1):017903.
- Sciarrino F, Lombardi E, Milani G, De Martini F (2002) Delayed-choice entanglement swapping with vacuum-one-photon quantum states. *Phys Rev A* 66:024309.
- Jennewein T, Aspelmeyer M, Brukner Č, Zeilinger A (2005) Experimental proposal of switched delayed-choice for entanglement swapping. *Int J Quant Inf* 3:73–79.
- Ma XS, et al. (2012) Experimental delayed-choice entanglement swapping. *Nat Phys* 8:480–485.
- Ionicioiu R, Terno DR (2011) Proposal for a quantum delayed-choice experiment. *Phys Rev Lett* 107(23):230406.
- Tang JS, et al. (2012) Realization of quantum Wheeler’s delayed-choice experiment. *Nat Photonics* 6:600–604.
- Peruzzo A, Shadbolt PJ, Brunner N, Popescu S, O’Brien JL (2012) A quantum delayed-choice experiment. *Science* 338(6107):634–637.
- Kaiser F, Coudreau T, Milman P, Ostrowsky DB, Tanzilli S (2012) Entanglement-enabled delayed-choice experiment. *Science* 338(6107):637–640.
- Ma XS, Qarry A, Kofler J, Jennewein T, Zeilinger A (2009) Experimental violation of a Bell inequality with two different degrees of freedom of entangled particle pairs. *Phys Rev A* 79:042101.
- Ma XS (2010) Nonlocal delayed-choice experiments with entangled photons. PhD Thesis (University of Vienna, Vienna, Austria).
- Kwiat PG, et al. (1995) New high-intensity source of polarization-entangled photon pairs. *Phys Rev Lett* 75(24):4337–4341.
- Grangier P (1986) Etude expérimentale de propriétés non-classique de la lumière; interférences à un seul photon [Experimental study of non-classical properties of light; single-photon interferences]. PhD Thesis (Institut d’Optique et Université Paris 11, Paris, France). French.
- Ballentine LE (1998) *Quantum Mechanics: A Modern Development* (World Scientific, Singapore), pp 256.
- Jennewein T, Achleitner U, Weihs G, Weinfurter H, Zeilinger A (2000) A fast and compact quantum random number generator. *Rev Sci Instrum* 71:1675–1680.
- Bell JS (2004) *Speakable and Unsayable in Quantum Mechanics* (Cambridge Univ Press, Cambridge), Rev. Ed.
- Scheidl T, et al. (2010) Violation of local realism with freedom of choice. *Proc Natl Acad Sci USA* 107(46):19708–19713.
- Greenberger DM, Yasin A (1988) *Phys Lett A* 128:391–394.
- Englert BG (1996) Fringe visibility and which-way information: An inequality. *Phys Rev Lett* 77(11):2154–2157.
- Ursin R, et al. (2007) Free-space distribution of entanglement and single photons over 144 km. *Nat Phys* 3:481–486.
- Ferriuzzi A, et al. (2009) High-fidelity transmission of entanglement over a high-loss free-space channel. *Nat Phys* 5:389–392.
- Salart D, Baas A, Branciard C, Gisin N, Zbinden H (2008) Testing the speed of ‘spooky action at a distance.’ *Nature* 454(7206):861–864.
- Weihs G, Jennewein T, Simon C, Weinfurter H, Zeilinger A (1998) Violation of Bell’s inequality under strict Einstein locality conditions. *Phys Rev Lett* 81:5039–5043.