

Nonpolar solutes enhance water structure within hydration shells while reducing interactions between them

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Edited by Bruce J. Berne, Columbia University, New York, NY, and approved March 24, 2005 (received for review January 10, 2005)

The origins of the hydrophobic effect are widely thought to lie in structural changes of the water molecules surrounding a nonpolar solute. The spatial distribution functions of the water molecules surrounding benzene and cyclohexane computed previously from molecular dynamics simulations show a high density first hydration shell surrounding both solutes. In addition, benzene showed a strong preference for hydrogen bonding with two water molecules, one to each face of the benzene ring. The position data alone, however, do not describe the majority of orientational changes in the water molecules in the first hydration shells surrounding these solutes. In this paper, we measure the changes in orientation of the water molecules with respect to the solute through spatial orientation functions as well as radial/angular distribution functions. These data show that the water molecules hydrogen bonded to benzene have a strong orientation preference, whereas those around cyclohexane show a weaker tendency. In addition, the water–water interactions within and between the first two hydration shells were measured as a function of distance and “best” hydrogen bonding angle. Water molecules within the first hydration shell have increased hydrogen bonding structure; water molecules interacting across shell 1 and shell 2 have reduced hydrogen bonding structure.

hydrophobic effect | orientation

It is widely understood that the structural changes in water induced by exposure to nonpolar surfaces are responsible for the phenomenon known as the hydrophobic effect (1). The small size, tetrahedral geometry, and hydrogen-bonding (H-bonding) ability of water all play a role in the interactions water takes part in with itself as well as with polar and nonpolar solutes. The structure of liquid water is well characterized experimentally in terms of radial distribution functions, $g(r)$, derived from diffraction experiments (2, 3). Similar experiments on solutions of alcohols and tetraalkylammonium ions, however, show very little structural differences in $g(r)$ compared with bulk water (2, 4). Yet the thermodynamics of insertion of nonpolar solutes into water show an unfavorable free energy, a positive entropy at room temperature, and a large positive heat capacity (5, 6). There are several possible reasons why the $g(r)$ may lack sensitivity in detecting structural changes in the hydration shells of hydrophobic solutes: (i) solubility of such solutes is small, so the majority of the observed signal arises from bulk water; (ii) solutes may be incompletely mixed (7); and (iii) the $g(r)$ is inherently insensitive to orientational structure.

The tetrahedral geometry of the water molecule and the directional nature of the H-bond impart a highly oriented structure to water. The orientational correlation function of liquid water has been generated by applying maximum entropy methods to $g(r)$ functions (8, 9). The resulting density distribution shows clear density peaks beyond the H-bond donor locations (along the O–H bonds), with a broader distribution in the acceptor positions (around the O). Very similar density patterns were seen in spatial distribution functions from water simulations (10, 11). Molecular

simulation has become an important tool for investigating the fine details of hydration structures of a variety of nonpolar solutes and surfaces (1, 12), including proteins (13). Specific studies of the orientational aspects of water structure around hydrophobic solutes of various sizes and shapes (14, 15) and surfaces (16) have been made. To summarize, the water molecules surrounding small solutes tend to make fewer but stronger H-bonds. Gallagher and Sharp (17) recently characterized the water structure around several solutes by using a radial/angular distribution function, an approach we have built on here. In this paper, we report several measures of the distribution of orientations of water molecules surrounding benzene and cyclohexane, with respect to both the solute and neighboring water molecules.

The hydration structure of benzene in water has been studied by using both molecular dynamics (MD) (18–20) and Monte Carlo (21–23) simulations. All of the simulations predict H-bonding to the benzene faces, with some variation in the binding energy and localization of the water above and below the ring. Previously, we described the spatially resolved structural details of the hydration structure of benzene and cyclohexane (18). Spatial distribution functions (SDFs) of the water density surrounding benzene and cyclohexane show a high-density first hydration shell and hints of a second shell. The SDF for benzene shows peaks above and below the benzene centroid that are not seen with cyclohexane. Comparison of the O and H atom SDFs for benzene indicates that water molecules in the axial peaks are oriented with an O–H bond pointing toward the solute centroid. The spatial data alone, however, do not detect changes in the water orientation due to the hydrophobic surfaces of the solute, the phenomenon we are most interested in exploring here.

In this paper, we investigate and compare the changes in orientation of water molecules as they hydrate cyclohexane and benzene. Two approaches were used: (i) spatially resolved measurements of the orientation of water molecules relative to the solute, and (ii) measurements of the water–water contact distance and angle within and between the first two hydration shells. The first approach includes computing spatial orientation functions (SOFs) and 2D radial distribution functions (resolved in tilt angle and distance). In the work presented here, both of these methods show that water molecules axial to benzene have a strong inward orientation. The majority of first shell waters around benzene and those surrounding cyclohexane, however, maintain considerable rotational degrees of freedom, yet show a weak tendency to point away from the solute.

The second approach complements the first because a nonpolar solute is thought to alter the water–water interactions in the surrounding shell. Quantification of these interactions involved classification of surrounding water molecules into discrete shells,

This paper was submitted directly (Track II) to the PNAS office.

Abbreviations: MD, molecular dynamics; DC, distance cutoff; VP, Voronoi polyhedra; SDF, spatial distribution function; SOF, spatial orientation function; S1, shell 1; S2, shell 2; B, bulk.

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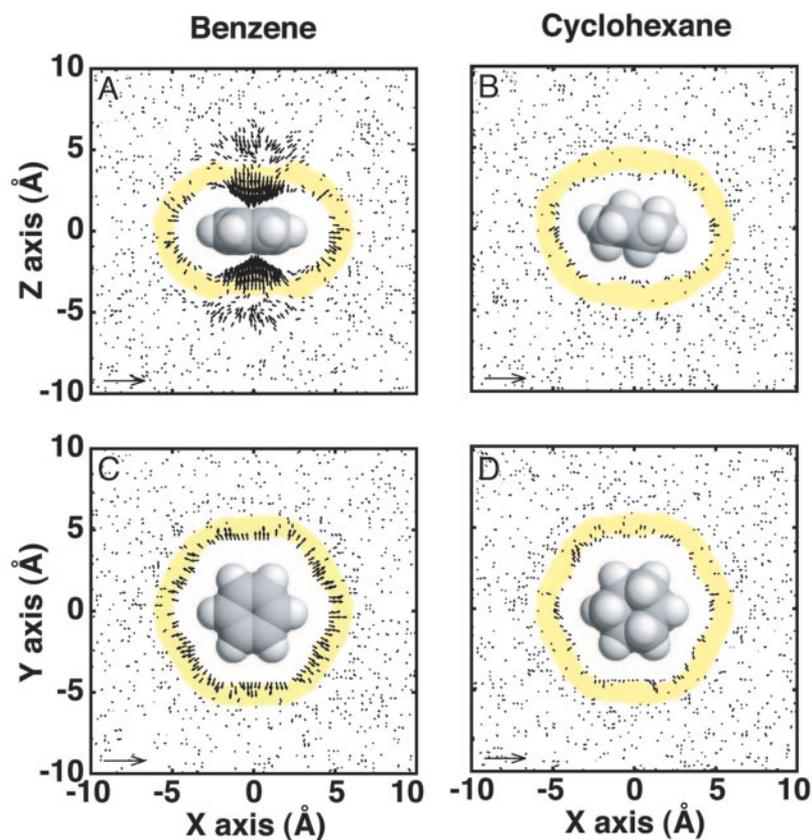


Fig. 1. SOFs of the water density surrounding benzene and cyclohexane. Slices through the volumes surrounding benzene and cyclohexane are shown. Projections of $\langle \vec{\mu} \rangle$, the time-averaged water orientation vector (see schematic in Fig. 2A), into the respective planes are drawn as arrows. The tail of each arrow originates from its corresponding voxel position, and the arrow length is proportional to the projection of $\langle \vec{\mu} \rangle$. Only the vectors with length greater than one standard deviation above the mean vector length in the dataset are graphed. A unit vector is drawn in the lower left corner for reference. The regions corresponding to the first hydration shells of the SDFs (above the $\rho_0 = 1.1$ density contour) are highlighted in yellow (A and B). The slice along the z - x plane for benzene (A) and cyclohexane (B). (C and D) The slice along the y - x plane for benzene (C) and cyclohexane (D).

Normalization of DC-Based Water–Water Contact Distance and Angle Distributions. For the DC-based shells, the distribution of distances and angles for all labeled waters was computed. The distribution was normalized in the contact length dimension to give $g_{OO}(r)$. For molecules that are spherically symmetric, $g(r)$ is normalized by assuming uniform bulk density in each spherical shell. For an asymmetric solute such as benzene or cyclohexane, such an analytical approach cannot be used. Thus, we generated an expected

distance distribution from a random sampling (36) of points distributed within (and between) the shell volumes observed in the MD simulations (see *Computational Methods*, which is published as supporting information on the PNAS web site).

Results

SOFs of Benzene and Cyclohexane. The SDFs of water molecules surrounding benzene and cyclohexane were previously published

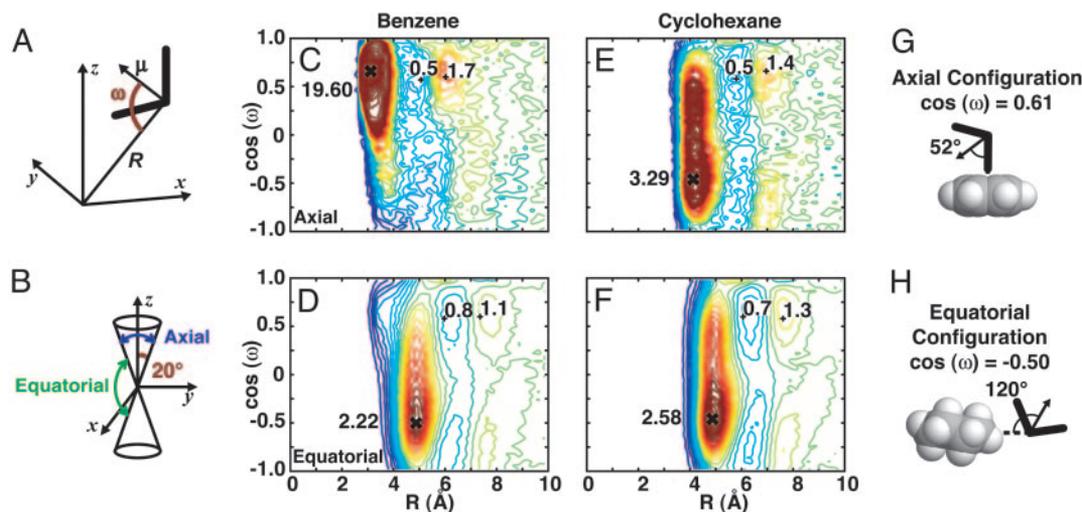


Fig. 2. 2D solute centroid to water oxygen radial distribution functions for benzene and cyclohexane. The radial-orientation distribution function, $g_{\text{Sol-O}}(R, \cos \omega)$ (where R is the distance to the center of the solute and the tilt angle ω is defined in A) averaged over the axial and equatorial volume regions (as defined in B) surrounding benzene are shown in C and D, respectively. Contours are drawn every 0.1 density unit relative to B (up to 3.0, and every 2.0 units between 4.0 and 20.0). The same functions for the axial (E) and equatorial (F) regions surrounding cyclohexane are also shown. Schematic diagrams show the preferred orientation of water molecules located axial to benzene (G) and equatorial to cyclohexane (H).

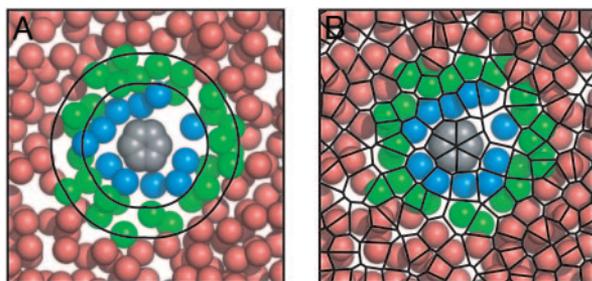


Fig. 3. Illustration of hydration shell assignments by the DC and VP methods. Shown is a snapshot of a 5-Å slice through the benzene simulation box. The benzene C atoms are gray, and the surrounding water O atoms are colored by class: S1, blue; S2, green; B, red. (A) Shell assignments based on the DC method. The black “circles” are arcs marking distances to the nearest solute C atom at the cutoff radii of 5.4 Å and 8.9 Å for S1 and S2, respectively. (B) Shell assignments based on the VP method. The 2D Voronoi tessellation of the projection into a plane illustrates how the box volume is divided into cells. Shell labels were based on contacts defined by the polyhedron faces (*Computational Methods*). The shell labels for individual water molecules may differ between the two methods.

(18). To complement that study, we computed the SOFs for the water molecules surrounding benzene and cyclohexane. Fig. 1 shows slices through the SOFs for both solutes. Projections of the longest $\langle \vec{\mu} \rangle$ vectors into the respective planes are drawn as arrows. The most striking feature of the benzene SOF (Fig. 1A) is the strong orientation of the water molecules located along the z -axis of the benzene; they have $\langle \vec{\mu} \rangle$ vectors that point directly toward the benzene centroid. This finding is consistent with our previous SDF results and the results of other simulations (19–23) and experiments (37, 38) that have shown a preference for H-bonding to the faces of the benzene ring. The axial ordering extends beyond the first hydration shell, with longer arrows seen further out along the z -axis, corresponding to second shell water molecules. In the equatorial region around benzene (Fig. 1C), the ordering is less pronounced. The $\langle \vec{\mu} \rangle$ vectors of the waters closest to the edge of benzene tend to point away from the solute, influenced by the localized positive charge in that region.

The SOF of the water molecules around cyclohexane is quite different from that of benzene. In Fig. 1B and D, the water molecules in the first hydration shell show less ordered $\langle \vec{\mu} \rangle$ vectors than those surrounding benzene. The water molecules closest to the cyclohexane show a slight tendency to point outwards, but the majority of the volume occupied by the first hydration shell is devoid of any long $\langle \vec{\mu} \rangle$. This finding indicates that ordering in the first hydration shell around a hydrophobic solute does not occur by forcing the waters into a fixed orientation; instead water molecules that occupy the same location in space sample a variety of orientations.

Radial/Angular Distribution Functions for Benzene and Cyclohexane.

To further explore the orientation preferences in the first hydration shell, we measured a combined solute–water radial/angular distribution function, $g_{\text{Sol-O}}(R, \cos \omega)$. Fig. 2 shows the $g_{\text{Sol-O}}(R, \cos \omega)$ for the axial and equatorial volume regions surrounding benzene and cyclohexane. Fig. 2C confirms that the water molecules axial to benzene occur at high density and with a strong inward orientation. The maximum of $\cos \omega$ in this region is 0.66, corresponding to $\omega = 48.7^\circ$. This value is very close to the expected value of 52.26° for orienting an O–H bond vector directly along \vec{R} (the H–O–H bond angle for TIP4P is 104.52°) (Fig. 2G). For the first hydration shell waters that are either equatorial to benzene (Fig. 2D) or axial or equatorial to cyclohexane (Fig. 2E and F), the orientation preference is less strong, but the maximum of $\cos \omega$ occurs between -0.46 to -0.50 , corresponding to an ω angle of 117 – 120° . This angle

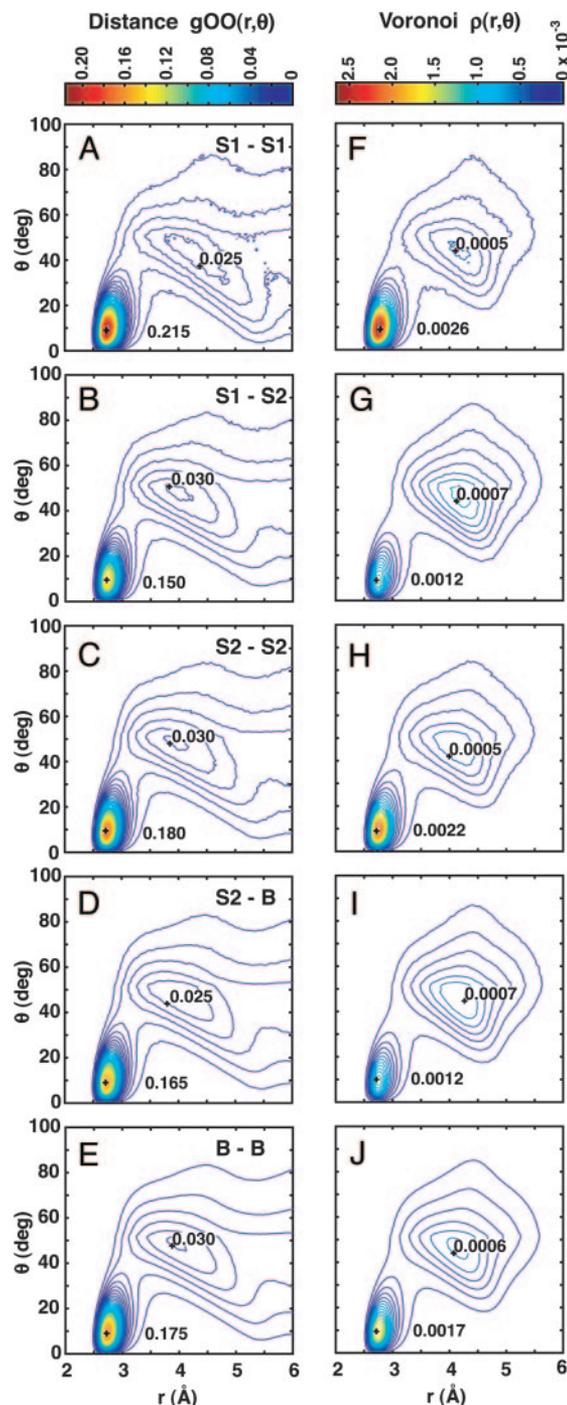


Fig. 4. Water–water contact length/angle distributions within and between the hydration shells of benzene. The distributions of water interaction geometries as a function of O–O distance (r) and minimum O–O–H angle (θ) between contacting water molecules are shown for five sets of inter- and intrashell interactions computed from the benzene simulations. The classes of interactions are S1–S1 (A and F), S1–S2 (B and G), S2–S2 (C and H), S2–B (D and I), and B–B (E and J). (Left) Shells determined by the DC method (A–E) and contours showing $g_{\text{OO}}(r, \theta)$. (Right) Shells and contacts determined by the VP method (F–J). In this case, the contours show the probability of observing contacts with particular geometries, $\rho(r, \theta)$. Angle, θ , measures the deviation from linearity of the least distorted H-bond.

positions an O–H bond vector roughly tangential to the surface of the solute, allowing for formation of a H-bond network within the first hydration shell (Fig. 2H).

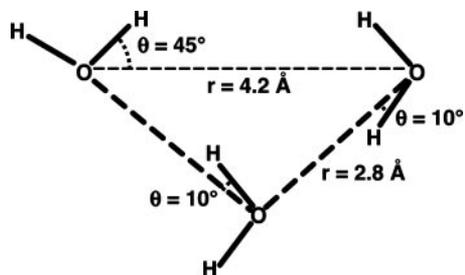


Fig. 5. A water “triangle” that occurs commonly in pure water. It explains both peaks in Fig. 4A. This figure also illustrates how the O...O distance (r) and minimum O...O-H angle (θ) are defined.

Identification of Hydration Shells by Voronoi Contacts and Cutoff Distances.

To test the assumption that the tangential orientation preference of the water molecules in the first hydration shell surrounding a hydrophobic solute allows for enhanced H-bonding, we decided to rigorously quantify the first and second hydration shells surrounding benzene and measure the H-bonding structure within and between the shells. For the DC method, the average number of water molecules in S1 for benzene was 31, and in S2 it was 98. The average number of hydration shell waters determined by VP was similar to DC, with 33 waters in S1 and 99 in S2 for benzene. An illustration of the shell assignments for a single MD frame is shown in Fig. 3. While there is significant overlap in the shell assignments between the VP and DC methods, some differences in labeling are observed.

Water–Water Contact Distance and Angle Distributions for Interactions Within and Between Hydration Shells. The distributions of water pair O...O distances (r) and minimum O...O-H angles (θ) were measured for all inter- and intrashell contacts. For the DC method, all water molecules positioned within 6 Å of each other were considered in contact. The $g_{OO}(r, \theta)$ distributions for the five classes of water interactions found by using the DC method of shell labeling on the benzene simulations are shown in Fig. 4A–E. Each graph has a characteristic shape, with a tall peak at short r and low θ (maximum at 2.7 Å and $\approx 9^\circ$), and a shorter, wide peak at longer r and a broader distribution of angles (maximum at 3.9–4.3 Å and 42.5–49.5°). The first peak corresponds to H-bonded water pairs, and the second peak corresponds to contacting waters that are not H-bonded to one another but are instead both H-bonded to a third water molecule (Fig. 5). The largest differences are seen between the S1–S1 distribution and the other classes of contacts. Within S1, the population of water molecules that fall within the H-bonding geometry is larger than that within the other classes. The H-bonding peak is lowest in the S1–S2 distribution, but the remaining three classes, S2–S2, S2–B, and B–B, are nearly identical to each other.

The distributions of water O...O distances and minimum O...O-H angles, $\rho(r, \theta)$, for the VP method applied to the benzene simulations are shown in Fig. 4F–J. The VP distributions have a shape similar to that of the DC distributions. The primary peak has a maximum at $r = 2.8$ Å and $\theta = 8.5$ – 10.5° , and the secondary peak is at $r = \approx 4.2$ Å and $\theta = 42.5$ – 48.5° . The relative height of the second peak is more pronounced because it is not flattened by normalization as is the case in a typical $g(r)$. The shapes of the boundaries of the distributions at longer contact length ($r > 5.4$ Å) are determined by the implementation of the Voronoi construction used (35), which will not allow any two water molecules separated by a distance that would accommodate an intervening water molecule to be in contact.

The water structure distributions for the VP-based shells show structural differences between the five classes of interactions. The S1–S1 interactions show the most H-bonding structure, with the largest difference between the first and second peak heights.

Likewise, the S2–S2 interactions show enhanced H-bonding, relative to the B–B interactions. Interestingly, the interactions between S1 and S2 show reduced H-bonding, with the majority of the population falling into the second peak. A similar pattern is seen in S2–B. These results show enhanced H-bonding structure within the first and second hydration shells, accompanied by decreased structure between them. While the DC method shows that the interactions within S1 are enhanced, the reduced structure in S1–S2 is observable, but more subtle. The results obtained for the cyclohexane simulations (not shown) were practically identical to those of benzene.

Fig. 6 shows for benzene the 2D water structure distributions

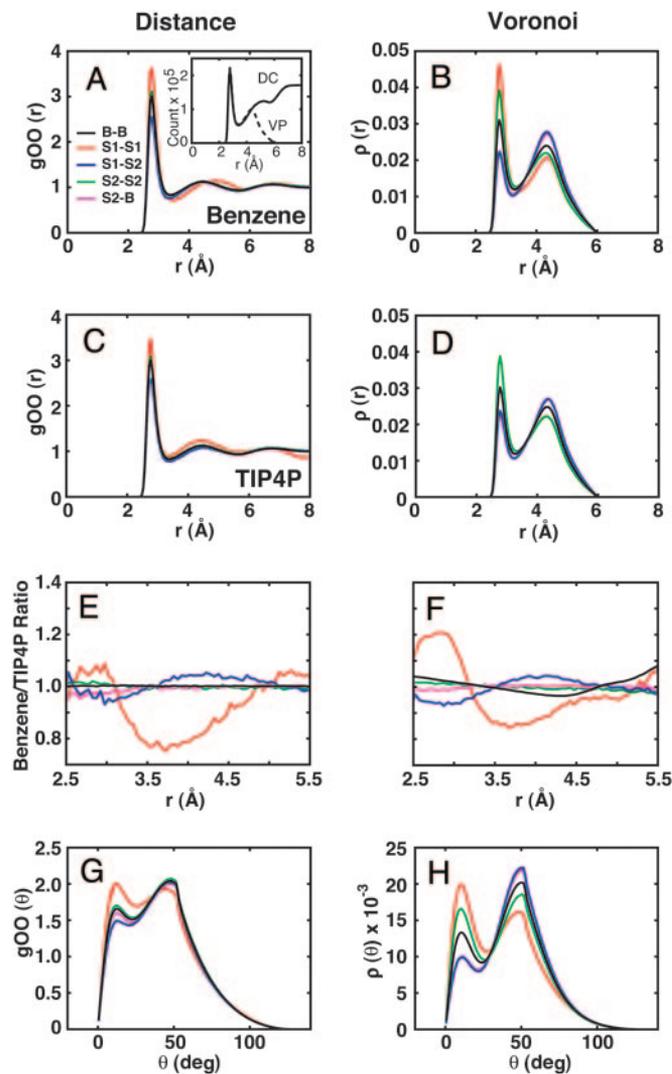


Fig. 6. Water–water radial distribution functions and contact angle distributions for the hydration shells of benzene determined by the DC and VP methods. The 2D distributions (Fig. 4) were summed over θ for each contact length, r , to give $g_{OO}(r)$ and $\rho(r)$ (A and B). The 2D distributions were also summed over r for each contact angle, θ , to give $g_{OO}(\theta)$ and $\rho(\theta)$ (G and H). Shell assignments were determined by the DC method (Left) or the VP method (Right). We distinguish by color five sets of interactions between water molecules: S1–S1, red; S1–S2, blue; S2–S2, green; S2–B, blue; and B–B purple. The Inset in A gives the unnormalized distributions of contact counts vs. r for the DC (solid line) and VP (dashed line) methods for the S1–S1 interactions, confirming the overlap of the two methods. (C and D) Length distributions for shells surrounding a single water molecule from control simulations of pure TIP4P water. (E and F) Benzene length distributions normalized by dividing by the TIP4P results.

from Fig. 4 projected into either the r or θ dimension. The results for cyclohexane (not shown) are indistinguishable from those of benzene. While both the VP and DC methods show an increase in H-bonds within S1 coupled with a reduction of H-bonds between S1 and S2, the changes are much more marked for the VP method (Fig. 6 *A* and *B*). In addition, the VP method shows an increase in H-bonding within S2 coupled with a reduction of H-bonds between S2 and B. Similar trends are seen for the angular distributions, with the height of the first peak measuring the extent of H-bonding (Fig. 6 *G* and *H*). The assignment of shell labels by using either the DC or VP method selects for water molecules that fall within geometrically defined volumes. The results shown in Fig. 4, therefore, may be influenced by these geometric restraints. To better understand these effects, we applied our analysis methods to a control simulation of pure TIP4P water molecules, specifying a single water molecule as the “solute.” The resulting measures of shell interaction geometries (Fig. 6 *C* and *D*) show that there are structural differences within and between the hydration shells of a single water molecule defined by both methods. Ratios of first and second peak heights for both solutes are given in Table 1, which is published as supporting information on the PNAS web site. Both methods show an apparent increase in the tangential H bonds within S1. In addition, the VP method shows similar results within S2. Both methods also show an apparent decrease in radial H-bonds (between S1 and S2). At present, we do not understand the cause of this geometric effect. We can, however normalize for this bias by dividing the benzene results by those for pure water (Fig. 6 *E* and *F*). These normalized distributions still show that S1...S1 hydrogen bonds are increased, whereas the S1...S2 hydrogen bonds are decreased.

Discussion

The origins of the hydrophobic effect are intimately linked with the structural changes induced by a nonpolar solute in water molecules that surround it. In this paper, we have measured the effects of the hydrophobic solutes benzene and cyclohexane on the orientation preferences of the hydration shell water molecules. These results not only highlight the obvious ordering of water molecules H-bonded to benzene but also reveal subtle biases in orientation in the first hydration shell associated with the hydrophobic effect. A key observation of our work is enhanced H-bonding structure within the first hydration shells combined with reduced hydrogen bonding with the second shell.

The SOFs show that the $\langle \vec{\mu} \rangle$ of the water molecules in the axial regions of benzene are strongly oriented inward, providing confirmation of H-bonding with the faces of the ring. The two H-bonded waters are only a small subset of the ≈ 30 water molecules found in the first hydration shell. The water molecules closest to the edge of benzene have a weaker, yet detectable, bias for an outward orientation. This result makes sense in the context of the localized partial positive charge on the edge of the ring. This ordering is not seen evenly throughout the majority of the volume of S1, however, which has relatively few long $\langle \vec{\mu} \rangle$ vectors.

The SOF results for cyclohexane are interesting, showing less order than benzene, and a S1 that is not well populated with long $\langle \vec{\mu} \rangle$ vectors. There is no strong absolute orientation bias induced in S1 by cyclohexane, and the water molecules in this region maintain significant rotational degrees of freedom.

Whereas the SOF shows relatively little orientation structure, $g_{\text{Sol-O}}(R, \cos \omega)$ is somewhat more sensitive to the structural biases of water near nonpolar solutes. In the regions around cyclohexane and equatorial to benzene, the water molecules sample a broad range of orientations, with the peak of the distribution corresponding to $\omega = 120^\circ$. This tilt angle would allow one O–H bond to orient roughly tangential to the solute surface, accommodating H-bonding with other S1 neighbors. Water molecules in the first hydration shell surrounding nonpolar surfaces, therefore, show a subtle but significant outward orientation preference.

Measuring H-bonding interactions within and between the hydration shells probes the orientation structure of water. Both the DC and VP methods show clear enhancement of the H-bonded population of neighboring waters in S1 and a reduction between S1 and S2. Thus, the strong H-bond network in S1 does not link the first and second shells.

The use of VP to identify both the shell labels and contacts of neighboring water molecules enhances the structural differences within and between the shells. The controls on pure water show this is a geometrical effect, which also occurs in a pure water control calculation. Our results emphasize the crucial role of controls in simulations and when using complicated geometrical procedures.

We thank Patrice Koehl for providing his Bestfit and Contact Area subroutines and Rachel Kolodny for helpful discussions. This work was supported by National Institutes of Health Grant GM-41455. M.L. was supported by the Fondation de l'École Normale Supérieure Chaires de Blaise Pascal.

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