

# Stretched exponential decay and correlations in the catalytic activity of fluctuating single lipase molecules

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Single-molecule techniques offer a unique tool for studying the dynamical behavior of individual molecules and provide the possibility to construct distributions from individual events rather than from a signal stemming from an ensemble of molecules. In biological systems, known for their complexity, these techniques make it possible to gain insights into the detailed spectrum of molecular conformational changes and activities. Here, we report on the direct observation of a single lipase-catalyzed reaction for extended periods of time (hours), by using confocal fluorescence microscopy. When adding a profluorescent substrate, the monitored enzymatic activity appears as a trajectory of “on-state” and “off-state” events. The waiting time probability density function of the off state and the state-correlation function fit stretched exponentials, independent of the substrate concentration in a certain range. The data analysis unravels oscillations in the logarithmic derivative of the off-state waiting time probability density function and correlations between off-state events. These findings imply that the fluctuating enzyme model, which involves a spectrum of enzymatic conformations that interconvert on the time scale of the catalytic activity, best describes the observed enzymatic activity. Based on this model, values for the coupling and reaction rates are extracted.

single enzyme activity | two-state trajectories

Dynamics of chemical reactions are conventionally investigated by ensemble measurements. Recent advances in single-molecule spectroscopy have enabled the real-time study of biophysical processes (1–10) and conformational changes (11, 12) of single biomolecules. These studies have demonstrated that new information about such processes can be extracted from single-molecule measurements. In particular, deviations from the standard Michaelis–Menten behavior (13, 14), which is expected for bulk enzymatic activity, have been observed (6–8, 12).

Motivated by these findings, we examined the enzymatic activity of individual molecules of the 33-kDa lipase B from *Candida antarctica* molecules (15, 16) by using confocal fluorescence microscopy. This lipase catalyzes the hydrolysis of esters in aqueous solution following the same reaction mechanism as that of a serine protease (17). To study the catalysis by single lipase, we used a fluorogenic substrate, namely the nonfluorescent ester 2',7'-bis-(2-carboxyethyl)-5-(and-6)-carboxyfluorescein acetoxymethyl ester, which upon hydrolysis forms a highly fluorescent carboxylic acid product (18, 19). This method enabled us to probe the enzymatic activity by monitoring the fluorescence emission from single enzymes. The fluorescence emission displayed blinking of “on” and “off” events depending on the presence (or absence) of the fluorescent product in the confocal focus (20). By using this approach, we have been able to obtain long trajectories (for time periods of hours) suitable for reliable statistical analysis while varying the

concentration of the substrate, thus allowing the study of the effect of changing the substrate concentration on the observed trajectories.

Our analysis demonstrates that the waiting time probability density function (PDF) of the nonfluorescent (off) state follows a stretched exponential with the same fitting parameters for a certain range of substrate concentrations. The highly nonexponential stretched behavior that is also evident in the state-correlation function is interpreted as a manifestation of a spectrum of active enzymatic conformations, which is supported by the oscillations in the logarithmic derivative of the off waiting time PDF. By performing previously undescribed methods of analyses on the data, we obtained information that is used to build a microscopic kinetic model most suitable to account for the experimental findings, namely the fluctuating enzyme model. Within the model, which involves both conformational changes and enzymatic activity, we were able to extract average values for the fast conformational fluctuations and reaction rates.

## Single Enzyme Measurements

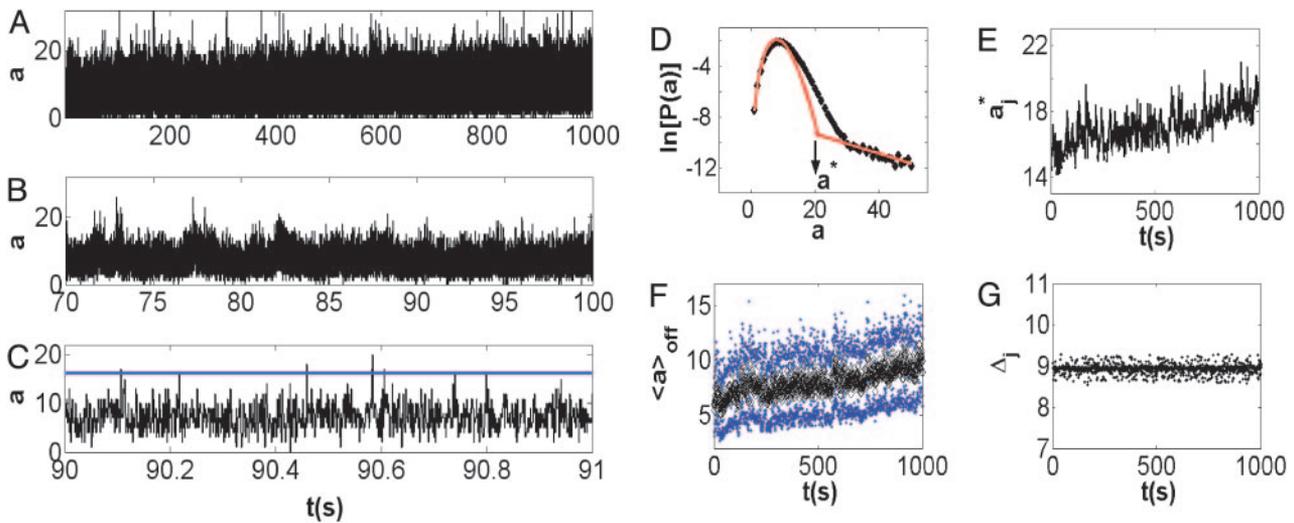
We start with a brief overview of the experimental setup. A full description is given in ref. 20. Individual lipase B molecules from *Candida antarctica* were nonspecifically labeled with Alexa Fluor 488 dye molecules (21, 22) and immobilized onto a surface derivatized with dichloro-dimethyl silane by using a hydrophobic glass. A laser-scanning stage confocal microscope was used to detect the lipase molecules. Focusing the laser on a single molecule, we used the attached dye fluorophores to zoom in on an enzyme molecule. The dye was then photobleached before the addition of the substrate. The recorded fluorescence emission showed a blinking (on/off) behavior, which was attributed to the enzymatic turnover cycle (ETOC). Several control measurements were performed to verify this conclusion (e.g., a signal was recorded from a system that contains enzyme in the absence of substrate and vice versa; see also ref. 20).

To analyze the recorded trajectories of the photon counts (Figs. 1A–C), the ETOC was viewed as a two-state process. The two distinct states are naturally defined by the absence (off state) and the presence (on state) of fluorescence emission. Note that the two-state picture is not an assumption but a consequence of the way the experiments were designed (20). The two-state ETOC dynamics is basically described by the waiting time PDFs of the off state,  $\phi_{\text{off}}(t)$ , and of the on state,  $\phi_{\text{on}}(t)$ . Namely,  $\phi_{\text{off}}(t)dt[\phi_{\text{on}}(t)dt]$  is the probability that a given off (on) event along the trajectory lasts between  $t$  and  $t + dt$ . In principle, these

Abbreviations: ETOC, enzymatic turnover cycle; PDF, probability density function; TSSM, two-state semi-Markov.

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**Fig. 1.** The photon count trajectory and its analysis. (A) A photon count trajectory as a function of time ( $\Delta t = 1$  ms) of a single lipase B from *Candida antarctica* during catalysis. (B and C) Zooming into segments of the trajectory in A. A local threshold value is shown in C. (D) A ln-linear histogram of  $P(a)$  (black curve). The arrow indicates the threshold value,  $a^*$ . Also shown are the fitting functions for the two parts of  $P(a)$  (red curves). (E) The floating threshold  $a_j^*$  as a function of time measured in bins of 1s ( $J = 1$ s). (F and G)  $\langle a_j \rangle_{\text{off}} \pm \sigma_j$ , the black sign corresponds to  $\langle a_j \rangle_{\text{off}}$ , and the blue sign corresponds to  $\pm \sigma_j$ , as a function of  $t$  with  $J = 1$  s (F), and the corresponding  $\Delta_j$  (G). In all figures,  $[S] = 1.4 \mu\text{M}$ .

functions do not fully describe the process (O.F., J.K., and A. Szabo, unpublished data). However, they do give its basic characteristics, primarily the number of substates in each of the states of the kinetic scheme. Based on our findings, we suggest below a kinetic scheme for the enzymatic activity.

To get  $\phi_{\text{off}}(t)$  and  $\phi_{\text{on}}(t)$ , the photon count trajectory  $[a(t)]_{t=0}^X$  (Fig. 1 A–C), where  $a(t)$  is a random photon count value at time  $t = i\Delta t$  ( $\Delta t = 1$  ms) and  $X$  is the measurement time (length of the trajectory), is transformed into a two-state (digital) trajectory. This transformation should be performed by applying on the trajectory a threshold photon count value  $a^*$ . Namely, by using  $a^*$ , the two states composing the trajectory were separated, so that each  $a(t)$  was attributed either to an off state,  $a_{\text{off}}(t)$  for  $a(t) < a^*$ , or an on state,  $a_{\text{on}}(t)$  for  $a(t) \geq a^*$ . To estimate  $a^*$ , we constructed the stationary histogram of the recorded photon counts  $P(a)$  (Fig. 1D).  $P(a)$  was composed of two contributions, a peaked off-state noise part and a monotonically decaying on-state part. The noise off-state part of  $P(a)$  was fitted with a Poisson PDF (although a Gaussian PDF fits equally well this part). The noise off-state part did not provide any information about the enzymatic process because it originates from background processes. The on-state part of  $P(a)$  was fitted by an exponential decay. This part did supply information about the enzymatic activity because it reflected the escape of the “newly formed” fluorescent product molecule from the enzyme and its vicinity. For example, the combination of an exponential on-state waiting time PDF and a Poissonian photon statistics leads to an exponential decay photon counts per bin for a wide range of parameters (O.F. and J.K., unpublished data). In this sense,  $P(a)$  shape supports the two-state picture. Now, the intersection between the two fitting functions of the two parts of  $P(a)$  can provide estimation for  $a^*$  (Fig. 1D). However, another complication prevents such a straightforward use of  $a^*$ . This complication is the increase in the noise level as the reaction progresses, which is attributed to the accumulation of the product molecules. To handle this issue, we performed a separate local treatment on the photon count trajectory to transform it into a digital trajectory. The photon count trajectory was divided into  $L$  intervals of duration  $J = X/L = 1$  s. In each  $\{j\}_{j=1}^L$  interval, the average  $\langle a_j \rangle_{\text{off}}$  and standard deviation  $\sigma_j = \sqrt{\langle a_j^2 \rangle_{\text{off}} - \langle a_j \rangle_{\text{off}}^2}$  of the off-state photon counts were calculated by using first

$a_1^* < a^*$ . Defining  $\Delta_j = a_j^* - \langle a_j \rangle_{\text{off}}$  and  $\delta_j = \sigma_j / \Delta_j$ , iterations were performed in each  $j$  interval until the local threshold  $a_j^*$  was such that the inequality  $\Delta_1 - \delta_j \leq \Delta_j \leq \Delta_1 + \delta_j$  was fulfilled.  $\Delta_1$  was chosen as a reference value because it defines a zero product trajectory accumulation. We note that  $a_1^*$  was chosen to be smaller than the intersection value because  $P(a)$  already contains contribution from the product accumulation. For example, to transform the trajectory shown in Fig. 1 A–C into a digital trajectory, we used several values for  $a_1^*$ ,  $a_1^* = 15, 16, 17$ , in the algorithm presented above. All three values for  $a_1^*$  led to digital trajectories with the same statistical properties.

By using the above algorithm, we fixed the difference between the average of the off photon counts and the threshold value along the trajectory within some small fluctuations window, whose width was set by the local features of the  $j$  interval. This algorithm resulted in a shift (on average) of the threshold to higher values as the reaction progressed (Fig. 1E) ( $j$  increased) while taking into account the basic characteristics of the noise part of  $P(a)$ . Shown in Fig. 1F and G are  $\langle a_j \rangle_{\text{off}} \pm \sigma_j$  and  $\Delta_j$ , respectively.

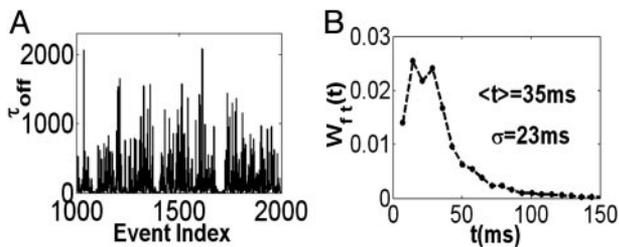
When applying this method, the photon count trajectory is translated into a digital trajectory whose statistical properties can be analyzed. We stress that the threshold value method used here provides reliable results for  $\phi_{\text{off}}(t)$  and  $\phi_{\text{on}}(t)$  for a fairly wide range of photon count parameters (O.F. and J.K., unpublished data).

### Statistical Analysis of the Digital Trajectory

The digital trajectory is characterized by the random process  $\{\xi(t)\}_{t=0}^X = 0, 1$ , made of on,  $\xi = 1$ , and off,  $\xi = 0$ , values.  $\phi_{\text{off}}(t)$  and  $\phi_{\text{on}}(t)$  can be constructed by building a histogram from the time durations of the corresponding events along the trajectory. Fig. 2A shows  $\phi_{\text{off}}(t)$  on a ln-linear scale for a set of three different substrate concentrations,  $[S] = 0.6, 0.9,$  and  $1.4 \mu\text{M}$ , demonstrating that the relaxation patterns are nonexponential. All of the three curves correspond to the kinetic behavior of the same lipase molecule, obtained by the sequential addition of substrate while monitoring the enzymatic activity for  $\approx 30$  min for each  $[S]$ . The best fit for these curves is found to be a normalized stretched exponential function (23),

$$\phi_{\text{off}}(t) = \phi_0 e^{-(t/\tau)^\alpha}; \quad \phi_0 = 1 / \int_0^\infty e^{-(t/\tau)^\alpha} dt = \frac{\alpha/\tau}{\Gamma(1/\alpha)}, \quad [1]$$

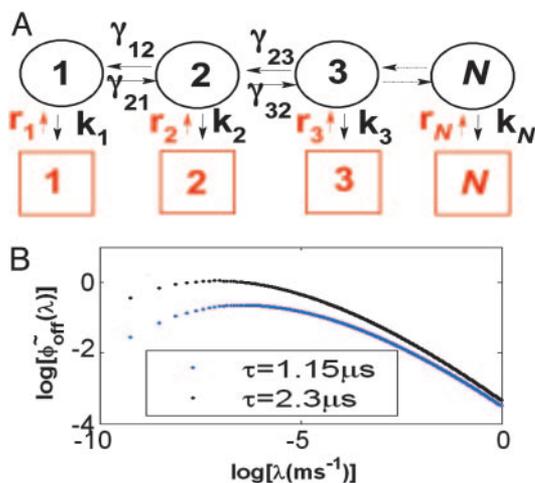




**Fig. 5.** The ordered off waiting times trajectory. (A) The trajectory of the time durations of the off-state events as a function of chronological event index for  $[S] = 1.4 \mu\text{M}$ . Noticeable along this trajectory are groups of successive fast events (each event in the group has a  $\tau_{\text{off}}$  value of  $<35$  ms). (B) The histogram of the time durations of the groups of successive fast events,  $W_{fit}(t)$ .  $W_{fit}(t)$  estimates the PDF to occupy a fast conformation (or conformations) for a time duration  $t$  before conformational changes occur.

event, where the events appear in the same order of their occurrence in the original time-series. A nontrivial correlation function calculated from this trajectory, which was used in ref. 6, and treated theoretically in O.F., J.K., and A. Szabo (unpublished data) and in refs. 29–31, serves, in principle, as an indication for conformational changes. In our case, the second point of such correlation function, which measures the correlation between successive events,  $R(1) = [\langle t_{\text{off},1} t_{\text{off},2} \rangle - \langle t_{\text{off}} \rangle^2] / [\langle t_{\text{off}}^2 \rangle - \langle t_{\text{off}} \rangle^2]$ , has a value of  $R(1) = 0.35$ . However, it is difficult to relate this quantity to the details of a kinetic scheme (see below). Nevertheless, by using an alternative analysis method of the ordered off waiting times trajectory, we extract more precise information about the ETOC mechanism.

Observing the ordered off waiting times trajectory, we noticed local trends (for all three concentrations) where events of similar short durations followed each other. Namely, along this trajectory fast events (each event is faster than 35 ms) were clustered together, with an average of  $3.5 (\pm 1.1)$  events per group and an average duration time of  $10 (\pm 2)$  ms per event in the group. Binning the times of the fast successive events in each group, we obtained a set of random variables from which we constructed a histogram denoted by  $W_{fit}(t)$  (Fig. 5B). This histogram should be interpreted in view of a kinetic model. When considering our findings, the most natural choice for a kinetic model is the fluctuating enzyme model (Fig. 6A). With this model in mind,



**Fig. 6.** The fluctuating enzyme model and the generalized density of rates. (A) A schematic model of the enzymatic process. The off state consists of a spectrum of  $N$ -coupled substates. Also indicated are the coupling rates between the conformations and the enzymatic reaction rates. (B)  $\tilde{\phi}_{off}(k)$  for a stretched exponential  $\phi_{\text{off}}(t)$  with  $\alpha = 0.15$  and  $\tau = 1.15 \mu\text{s}$ , blue curve, and with  $\alpha = 0.15$  and  $\tau = 2.3 \mu\text{s}$ , black curve.

$W_{fit}(t)$  estimates the PDF to occupy a fast conformation (or conformations) for an overall duration  $t$ , in which several on/off cycles can occur, before conformational changes to a slow conformation is taking place.

### Modeling

Consider a Michaelis–Menten type of model of a three-stage reaction mechanism (13),



The symbols  $E$ ,  $S$ , and  $P$  stand for the enzyme, substrate, and product molecules, respectively, and the symbols  $ES$  and  $EP$  stand for the enzyme–substrate and enzyme–product complexes, respectively. In this model, the first two stages, which are the formation of the complex  $ES$  and the transformation of the substrate into product, constitute the off state. The third stage, which is the escape of the product away from the enzyme and its vicinity, constitutes the on state. The off waiting time PDF for this model does not lead to a stretched exponential waiting time PDF. In particular, given a high enough substrate concentration, the expression for  $\phi_{\text{off}}(t)$  is simply a biexponential [the expression for  $\phi_{\text{on}}(t)$  is a single exponential]. Thus, the observed trajectory requires going beyond the Michaelis–Menten type of description. As known from other systems (23, 25, 32, 33), a stretched exponential decaying pattern can arise from contributions of a large number of weighted exponentials. In the present case, the stretched exponential decay pattern of  $\phi_{\text{off}}(t)$  serves as an indication that the system exhibits dynamic disorder. In other words, the  $\phi_{\text{off}}(t)$  form, which is  $[S]$ -independent over some concentration range, indicates that a spectrum of enzymatic conformations is involved in the catalytic activity. Any suggested model should incorporate this feature.

We therefore consider a model that involves simultaneously enzymatic activity and conformational changes. The model describes an off state that consists of a broad spectrum of conformational substates, with nearest neighbors connectivity (Fig. 6A). The dynamics of the conformational changes are governed by the coupling rates  $\gamma_{m \pm 1m}$ , where  $\gamma_{m \pm 1m}$  is the coupling rate from conformation  $m$  to  $m \pm 1$ . Each of these conformations is active and can react with a reaction rate  $k_m$  for substate  $m$ . This picture is consistent with experiments that probe conformational changes in proteins and report on fingerprints of a large number of conformations (11). While conformational fluctuations take place, the enzyme–substrate complex is formed, where similar to the experimental conditions  $[S]$  is large enough to have always a substrate molecule in the vicinity of the enzyme; namely,  $[S]$  does not play a role in the dynamics of the off stage. Once the enzyme–substrate complex is formed the enzyme can react, transforming the substrate into a product, which terminates the off state. If we assume that the transformation of the substrate into a product is a fast process relative to the formation of the complex itself or its dissociation, then the appropriate kinetic scheme that underlies the studied enzymatic activity is the fluctuating enzyme model shown in Fig. 6A, where rate  $k_m$  can be still defined as a reaction rate of the enzymatic activity. The information extracted from the off ordered waiting times trajectory (the average number of successive fast events and the average time duration of a fast event) can be related to the average reaction rate of the fast conformations,  $\langle k \rangle_{\text{fast}} \approx (8 \text{ ms})^{-1}$ , and the average fluctuation rate from slow to fast conformations,  $\langle \gamma \rangle_{\text{fast} \rightarrow \text{slow}} \approx (45 \text{ ms})^{-1}$  (O.F., J.K., and A. Szabo, unpublished data).

The on-state time durations start when the product is formed and last until it escapes from the enzyme and its vicinity. If the formation of the product took place from conformation  $m$  in the off state, the escape process occurs with a reaction rate  $r_m$ , where we require  $r_m = \kappa$  for an exponential  $\phi_{\text{on}}(t)$ . We assume that conformational changes in the on state do not occur during

occupying the on state, or, alternatively, the coupling rate values are small compared with  $\kappa$  (which is in fact the case if we consider  $\langle \gamma \rangle_{\text{fast} \rightarrow \text{slow}}$  as an estimation of the fluctuating rate in the on state as well).

To relate  $\phi_{\text{off}}(t)$  to the fluctuating enzyme model, we write the expression for  $\phi_{\text{off}}(t)$  as,  $\phi_{\text{off}}(t) = A \sum_m \omega_m e^{-\lambda_m t}$ , where  $A$  is a normalization constant, the sum is taken over all possible substates, and  $\omega_m$  and  $\lambda_m$  are the weights and relaxation rates, respectively. Because of the coupling between the off substates, the dependence of  $\omega_m$  and  $\lambda_m$  on  $m$  involves all of the  $\gamma_{m \pm 1m}$ 's and the  $k_m$ 's. The continuum representation of  $\phi_{\text{off}}(t)$  for a large number of substates is given by

$$\phi_{\text{off}}(t) = \int_0^\infty \tilde{\phi}_{\text{off}}(\lambda) e^{-\lambda t} d\lambda; \quad \tilde{\phi}_{\text{off}}(\lambda) = A \omega(\lambda) \rho(\lambda),$$

[3]

where we introduce the density of rates,  $\rho(\lambda)$ . Hence,  $\tilde{\phi}_{\text{off}}(\lambda)$  is the inverse Laplace transform of  $\phi_{\text{off}}(t)$  (34, 35) and serves as a generalized density of rates. Fig. 6B shows the broad mono-peaked  $\tilde{\phi}_{\text{off}}(\lambda)$  obtained by numerically inverting the stretched exponential  $\phi_{\text{off}}(t)$ , with  $\alpha = 0.15$  and  $\tau = 1.15 \mu\text{s}$ , blue curve, and  $\alpha = 0.15$  and  $\tau = 2.3 \mu\text{s}$ , black curve. Both curves display a power law asymptotic decay pattern,  $\tilde{\phi}_{\text{off}}(\lambda) \sim \lambda^{-1-\alpha}$ , which is obtained by using the Tauberian theorem (36) for large enough  $\lambda$  values. In a recent article (12), a peaked distribution of reaction rates was extracted from single T4 Lysozyme TOC trajectories ( $\approx 50$ ), lasting  $\approx 20$  s. In our studies, each of the trajectories was long-lasting ( $\approx 30$  min) and consisted of contributions from the entire distribution, which leads to the nonexponential decay pattern of  $\phi_{\text{off}}(t)$ .

### Concluding Remarks

Nonexponential behavior of biomolecules has been obtained in several systems (11, 32, 33). Here, we report on a direct observation on the single-molecule level of a stretched expo-

ponential off waiting time PDF in the enzymatic catalytic activity of lipase B from *Candida antarctica*,  $\phi_{\text{off}}(t) \sim e^{-(t/\tau)^{0.15}}$  ( $\tau \approx 1 \mu\text{s}$ ). Searching for the origin of the stretched behavior, we ruled out the possibility of an external source such as the substrate concentration. The oscillations in the function  $G[\phi_{\text{off}}(t)]$  forced us to the conclusion that the off process is composed of a large number of subprocesses, which we interpreted as a spectrum of conformations, each of which contributes an exponential factor to the overall decay process. By confronting the experimental state-correlation function,  $C(t)$ , with a theoretical state-correlation function for a TSSM process with the experimental  $\phi_{\text{on}}(t)$  and  $\phi_{\text{off}}(t)$ , we concluded from the different behavior of these functions [in both cases  $C(t) = e^{-(t/\tau)^\beta}$  with similar  $\beta$  values ( $=0.085$ ) but with 3 orders of magnitude difference in the values of  $\tau$ ] that the underlying mechanism cannot be described as a TSSM process and that correlations between events exist. Indeed, the trajectory of the off time durations exhibited local trends of bunched fast events. We were, thus, led to describe the observed enzymatic activity by the fluctuating enzyme model (Fig. 6A). In light of this model, average values for the coupling and reaction rates were estimated,  $\langle \gamma \rangle_{\text{fast} \rightarrow \text{slow}} \approx (45 \text{ ms})^{-1}$  and  $\langle k \rangle_{\text{fast}} \approx (8 \text{ ms})^{-1}$ , respectively.

The analysis presented here is related to two basic questions in the context of two-state single-molecule trajectories: (i) what is the maximal amount of information that can be extracted from two-state trajectories about the underlying kinetic schemes; and (ii) how should the information be extracted? The case of single lipase molecules provided an example for dealing with these questions. A detailed theoretical treatment of what can be learnt from two-state single molecule trajectories will be published elsewhere (O.F., J.K., and A. Szabo, unpublished work).

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