Rethinking language: How probabilities shape the words we use

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If you think about the classes you expect to take when studying linguistics in graduate school, probability theory is unlikely to be on the list. However, recent work in linguistics and cognitive science has begun to show that probability theory, combined with the methods of computer science and statistics, is surprisingly effective in explaining aspects of how people produce and interpret sentences. How language might be learned (4–6), how words change over time (7, 8), and the role that words play in sentences (19) and inferring the structure of those sentences (20), and it is now difficult to understand most papers at a computational linguistics conference without a good education in statistics.

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A word. In this framework, the informativeness of a word is given by the negative logarithm of its probability, matching the intuition that less probable words carry more information. The return of probability theory to language slowed with the rise of Chomskyan linguistics. Chomsky (17) argued convincingly against the ability of Markov chains to capture the structure of sentences. His famous sentence “Colorless green ideas sleep furiously” was constructed, in part, to illustrate that Markov chains cannot be used to determine whether a sentence is grammatical: Each pair of words in this sequence is unlikely to occur together, so its probability should be near zero even though most speakers of English would agree it is grammatical (if a little unusual). This argument against a specific probabilistic model was taken to refute more generally the relevance of probability theory to understanding language, with formal linguistics turning to a mathematical framework that had more in common with logic.

The rise of probability theory to linguistics came via work on the more applied problem of making computers process human languages. Probability theory can be used to solve two kinds of problems: making predictions and making inferences. Both are relevant to processing language. If you want to do a good job of interpreting human speech, it helps to have a good model of which sequences of words you are likely to hear. Understanding sentences and learning language are both problems of inductive inference, requiring a leap that goes from the words we hear to an underlying structure, and probability theory (and particularly Bayesian inference) can be used to solve these problems. Computational linguists discovered that ideas from probability theory could improve algorithms for speech recognition (18), identifying the roles that words play in sentences (19) and inferring the structure of those sentences (20), and it is now difficult to understand most papers at a computational linguistics conference without a good education in statistics.

The Rise of Probability

Probability theory has begun to migrate from computational linguistics into other areas of language research. The problems posed by colorless green ideas can be circumvented by using more sophisticated probabilistic models than Markov chains (21), and theorists are beginning to ask whether probabilities appear in linguistic representations (22, 23). Psycholinguists have begun to examine how the predictability of a word influences its production and processing (1–3). Language learning researchers have used probability theory as the basis for theoretical arguments that language can be learned (4), as well as in experiments and models exploring the acquisition of its components (5, 6). Research on how languages change over time now has access to reconstructions of the relationships between languages (and the words themselves) produced using probability theory (7, 8). Supporting these probabilistic models is the availability of large amounts of linguistic data, through databases that are larger and easier to access than ever before.

Piantadosi et al. (9) draw on these resources to conduct a deeper analysis of the factors influencing the length of words. Their basic empirical result is a nice extension of Zipf’s original observation, showing that the length of words is not just

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related to their frequency but to their predictability in context. By considering the frequency of a word, Zipf measured how predictable that word is if you know nothing else about the words you are likely to encounter. However, Markov chains can be used to compute how probable each instance of a word is based on the last few words, providing a way to measure the predictability of a word in its context. This makes it possible to calculate how much information is contributed by that word, using the metric introduced by Shannon (16). If a word is easy to predict based on context, it contributes little information. Piantadosi et al. (9) find that the average information contributed by a word is better correlated with its length than is its overall frequency, suggesting that the predictability of a word in context is what matters in determining how long that word should be.

This refinement of our understanding of the relationship between the length of a word and its predictability is bolstered by a theoretical framework that adds precision to Zipf’s Principle of Least Effort and connects the relationship between word length and probability to an idea that has already proven valuable in other areas of psycholinguistics. This framework is based on the “Uniform Information Density” hypothesis: the idea that human languages follow the optimal strategy for communicating information through a noisy channel, by transmitting information at a constant rate that matches the capacity of the channel (2, 24–27). A crude analogy might be to imagine communication in terms of pumping oil along a fragile pipe. If you pump too slowly, it takes too long; pumping too quickly risks breaking the pipe; and varying the rate of flow is either inefficient or dangerous. The best strategy is to pump at a constant level set by the capacity of the pipe. In the case of language, we are pumping words at one another; the time it takes to send a word along the pipe is determined by its length, and the capacity of the pipe is determined by the rate at which we can process linguistic information. The best solution is to send information at a constant rate, which means that less predictable words, those that carry more information, should be longer.

The Uniform Information Density hypothesis shares with the Principle of Least Effort the notion of optimization, making the most of a limited resource, but gives this notion a formal precision that leads to a variety of other interesting predictions. For example, including an additional unnecessary word, such as “that,” in a sentence (e.g., “How big is the family that you cook for?”) potentially dilutes the information density of the sentence (specifically, the information associated with the clause beginning with “you”). The information density will thus become more uniform if such words are introduced to sentences that carry more information, and people’s word choices seem to follow this prediction (2). Explanations framed in terms of information density rather than least effort also make it clearer that we should imagine language as being tailored to fit human minds rather than human laziness.

Providing a formal framework connecting word length and predictability opens the door to further analyses using more sophisticated probabilistic models, and considering other statistics that might be relevant to understanding the lengths of words. There is still a great deal of variance in the length of words that is not explained by their predictability. However, the deeper message behind the results of Piantadosi et al. (9) is that probability and information theory can help us rethink the way that language works, and how it should be studied. Probabilities can augment the classic rule-based representations that are widely used in linguistics, and information theory provides a way to formalize ideas like the Principle of Least Effort in a way that leads to unique predictions about language. Conversely, perhaps judgment should be reserved until Uniform Information Density makes its own appearance in literary fiction.